

## Uncertainties on gamma-ray energies and intensities measured in the decay of $^{83}\text{Sr}$

Shuifa Shen<sup>\*,†,¶</sup>, Xiaohan Yu<sup>‡</sup>, Jiejie Shen<sup>§</sup>, Shuanghui Shi<sup>‡</sup>,  
Jingyi Liu<sup>‡</sup>, Wenxin Li<sup>‡</sup>, Yan Li<sup>‡</sup> and Yupeng Yan<sup>†</sup>

*\*Key Laboratory of Neutronics and Radiation Safety,  
Institute of Nuclear Energy Safety Technology,  
Chinese Academy of Sciences, Hefei 230031, Anhui, P. R. China*

*†School of Physics, Institute of Science,  
Suranaree University of Technology,  
Nakhon Ratchasima 30000, Thailand*

*‡Shanghai Institute of Applied Physics,  
Chinese Academy of Sciences,  
Shanghai 201800, P. R. China*

*§Institute of Pharmaceutical Biotechnology,  
College of Pharmaceutical Sciences,  
Zhejiang University, Hangzhou 310058, Zhejiang, P. R. China*  
*¶shuifa.shen@fds.org.cn*

Received 5 February 2017  
Accepted 27 February 2017  
Published 27 March 2017

We analyze once again the  $\gamma$  singles spectra and  $\gamma$ - $\gamma$ - $t$  coincidence spectra following the  $\beta^+$ +EC decay of  $^{83}\text{Sr}$ . Multipeaks are carefully separated and many  $\gamma$  transition cascades are clearly obtained in the work. As a complement to our previous work, the uncertainties on  $\gamma$ -rays energies,  $\gamma$ -rays intensities and deduced level energies in the  $\beta^+$ +EC decay of  $^{83}\text{Sr}$  are given now.

*Keywords:* Uncertainty on  $\gamma$ -ray energy; uncertainty on  $\gamma$ -ray intensity.

PACS Number(s): 29.85.Fj, 23.20.Lv, 27.50.+e

In our previous work,<sup>1</sup> approximately 190  $\gamma$ -rays including 94 new  $\gamma$ -rays and 19 new levels were assigned to the  $\beta^+$  + EC decay of  $^{83}\text{Sr}$ . Among the approximately 190  $\gamma$ -rays, 180 ones were placed in the decay scheme which incorporates all the observed  $\gamma$  transitions except seven relatively weak ones, but no uncertainties on  $\gamma$ -ray energies and intensities were given. Therefore, we analyze once again the  $\gamma$  singles in the multispectra mode and  $\gamma$ - $\gamma$ - $t$  coincidence spectra, by paying particular attention to the hardly decomposed  $\gamma$ -ray multiplets.

Details of the experimental procedure and main results can be found in Ref. 1, but some important points may be mentioned here for completeness. The summed

singles spectra are analyzed carefully with a computer program which fits each peak with an adjustable lines shape (approximately Gaussian), then the centroid channel and peak area are used to derive the  $\gamma$ -ray energy, intensity and their uncertainties. Many weak  $\gamma$ -rays which are not identified or barely assigned in each individual spectrum can be clearly identified in the summed singles spectrum. The relative intensities of  $\gamma$ -rays, including the energies of that below 60 keV, are determined from the summed spectrum without anti-Compton suppression. The energies of  $\gamma$ -rays above 60 keV are obtained from Compton-suppressed spectra.

The uncertainties of the  $\gamma$ -rays energy and intensity include the contributions from the counting statistics, the systematic uncertainty of the energy calibration and relative efficiency calibration, respectively, and the normalization procedure. For the singles spectrum, the systematic uncertainty of the energy calibration is 0.04 keV when the  $\gamma$ -rays energy is below 200 keV or over 2000 keV, otherwise it is 0.03 keV, while the systematic uncertainty of the relative efficiency calibration is 3% when the  $\gamma$ -rays energy is less than 250 keV and 2% when the  $\gamma$ -rays energy is larger than 250 keV. For the coincidence spectrum the systematic uncertainty of energy calibration is 0.1 keV and that of relative efficiency calibration is 5%. Now the uncertainties on  $\gamma$ -rays energies and intensities of all the  $\gamma$ -rays assigned to the decay of  $^{83}\text{Sr}$  are added, as shown in Tables 1 and 2. The reported uncertainties refer to the last significant digits.

Because both the energy resolution of spectrometer and the statistical fluctuation of counts have been largely improved, compared to the previous works, coupled with the use of detailed spectral decomposition method, the accuracy of energy measurement is improved by over three times. By decomposing the multiple peaks, a number of new  $\gamma$ -rays are discovered. The background and contaminants at very low radioactive level are mainly  $^{85}\text{Sr}$ ,  $^{83}\text{Rb}$ ,  $^{84}\text{Rb}$ ,  $^{131}\text{Ba}$ ,  $^{60}\text{Co}$ ,  $^{40}\text{K}$ ,  $^{137}\text{Cs}$ , etc. The energies and uncertainties of all 41 excited levels (see Table 1) are obtained by the method of least squares. Table 2 is the same as Table 1 in our previous paper,<sup>1</sup> but now the uncertainties are added. It should be noted here that we provide  $I_\gamma$  in this paper, but in Fig. 2 of our previous paper<sup>1</sup> the data next to the  $\gamma$ -rays energy are the transition intensities, as implied by the words “Intensities:  $I_{(\gamma+ce)}$  per 100 parent decays”, where  $I_{ce}$  ( $I_{ce}$  denotes the intensity of internal-conversion electron) is obtained from the calculations. The measured energy region is between 30 keV and 2650 keV, thus the 42.08 keV  $\gamma$ -ray can be detected and its uncertainty is also given, as shown in Table 1, but not the 5.23 keV  $\gamma$ -ray.<sup>2</sup>

All the intensities of the  $\gamma$ -rays are normalized to an intensity of 100 for the 762.61 keV  $\gamma$  transition. An additional measurement of the relative intensity of the 511 keV annihilation radiation (from which the total  $\beta^+$  decay intensity can be obtained) is performed, with the  $^{83}\text{Sr}$  source sandwiched between two lead plates of 3 mm thickness each, to produce total annihilation. The relative ( $\beta^+ + \text{EC}$ ) decay strength (normalized to intensity of 762.61 keV  $\gamma$  transition) to each excited level can be obtained from intensity balance. By using theoretical  $I_{\beta^+}/I_{\text{EC}}$  values, the relative  $\beta^+$  intensity of each excited level can be calculated. The relative intensity

Table 1. The uncertainties of energies and relative intensities of  $\gamma$ -rays assigned to the decay of  $^{83}\text{Sr}$  and placed in the decay scheme and the deduced uncertainties of level energies.

$E_x$ (keV)	$I^\pi$	$E_\gamma$ (keV)	$I_\gamma$	$E_x$ (keV)	$I^\pi$	$E_\gamma$ (keV)	$I_\gamma$	$E_x$ (keV)	$I^\pi$	$E_\gamma$ (keV)	$I_\gamma$
2189.54523	9/2+	2147.426	0.564 12			1492.785	0.0655	678.314	0.1536		
		1765.845	0.0593	1798.475 18	(5/2)+	1798.464	0.1014	438.163	2.906		
		1452.507	0.0273			1793.236	0.0382	159.654	0.373 19		
		1395.959	0.0313			1756.384	0.0753	1201.955 18	(5/2,7/2)+	1201.943	0.4239
		1384.834	0.3449			1374.864	0.1805	1159.873	5.1410		
		1151.979	0.0176			1233.945	0.0673	778.383	6.5813		
		1086.674	0.0985			993.783	1.233	737.33	0.0201		
		987.609	0.0323			715.353	0.339 12	637.397	0.0574		
		764.925	0.2176			555.6313	0.0275	1102.814	9/2-	1102.734	0.1104
		494.15	0.0503	1749.252 18	(5/2+,7/2)	1749.204	0.0914	365.52	0.0258		
2134.70524	(5/2,7/2)+	2134.676	0.0933			1707.155	0.0773	1096.459 24	(9/2)+	1054.333	0.726 16
		2092.4617	0.0051			1325.624	0.2567	673.046	0.0747		
		1711.124	0.1115			1184.5410	0.0183	291.617	0.0879		
		1397.569	0.0413			944.513	0.443 11	1083.132 23	(1/2,3/2)+	659.533	0.810 18
		1330.039	0.0263			652.783	0.2817	1037.653	11/2+	995.554	0.545 12
		1038.234	0.3017			547.34	0.0301	243.94	0.0502		
		838.7812	0.0186			506.42	0.263	1035.118 23	(3/2,5/2)	1035.044	0.1284
		768.908	0.0263	1695.334 24	(7/2,9/2)+	1653.224	0.2547	1029.6317	0.0112		
		537.127	0.0348			1271.814	0.2337	935.796	0.0525		
2094.985	(5/2+,7/2,9/2)	2052.937	0.0281			890.603	0.449 11	645.744	0.185 10		
		1290.2311	0.0162			657.684	0.3238	611.42	0.0214		
		892.967	0.0483			599.1213	0.0187	568.007	0.0135		
		2089.715	0.4009			493.455	0.196 11	470.699	0.0268		
2089.72519	(5/2,7/2+)	2047.645	0.3227			270.82	0.0301	298.025	0.0926		
		1666.164	0.2818	1649.354	(5/2,7/2,9/2)-	1649.405	0.0863	1010.203	(3/2,5/2,7/2)-	1010.184	0.1295
		1525.2226	0.0051			1084.767	0.0403	1004.964	0.0944		
		1352.4610	0.0345			827.8114	0.0155	445.697	0.0585		
		1285.024	0.3068			795.345	0.0763	907.947 22	(3/2,5/2)	907.945	0.723 22
		993.225	0.16717			639.138	0.0514	902.644	0.1825		
		846.874	0.1935	1614.764	(5/2+,7/2,9/2+)	1572.705	0.0432	808.604	0.1685		
		812.3213	0.0213			1191.1013	0.0142	518.52	0.112		

Table 1. (Continued)

$E_x$ (keV)	$I^\pi$	$E_\gamma$ (keV)	$I_\gamma$	$E_x$ (keV)	$I^\pi$	$E_\gamma$ (keV)	$I_\gamma$	$E_x$ (keV)	$I^\pi$	$E_\gamma$ (keV)	$I_\gamma$
		723.72 13	0.016 3			1050.24 4	0.318 7			484.5 5	0.020 2
		394.47 12	0.026 4			877.63 5	0.082 3			440.85 8	0.042 5
2056.93 4	(5/2+, 7/2+, 9/2)	2014.83 4	0.145 4			371.9 3	0.022 6			343.4 3	0.030 2
		1319.84 11	0.013 2		(3/2, 5/2, 7/2)	1606.07 14	0.008 2			853.953 19	(3/2, 5/2)
		1252.30 5	0.049 5			1600.97 9	0.020 2			848.66 3	0.592 13
		1019.25 4	0.176 7			1506.91 8	0.022 2			754.56 5	0.103 4
2036.40 10	(5/2, 7/2)	2030.99 15	0.008 1		(5/2, 7/2)	1597.59 4	0.111 5			289.53 5	0.122 7
		1647.21 15	0.012 2			1592.31 5	0.039 2			821.61 3	(3/2, 5/2)
		1612.70 12	0.034 3			1208.17 5	0.062 3			816.34 4	0.168 5
		1231.85 12	0.008 3			1173.88 4	0.171 7			722.28 7	0.044 3
1951.918 13	5/2+	1951.93 3	2.71 5			792.97 4	0.122 4			804.67 3	0.308 7
		1946.66 5	0.065 2			395.62 4	0.209 10			762.61 3	100
		1562.53 3	6.07 12		(9/2+)	1382.73 5	0.131 4			381.09 5	6.71 20
		1528.34 4	0.332 8			630.88 5	0.087 8			751.71 4	0.193 5
		1387.38 5	0.085 3		(3/2, 5/2)	1275.34 8	0.029 3			737.07 3	0.875 19
		1214.79 3	0.850 19			907.62 10	0.021 8			731.84 3	0.296 7
		1147.17 3	4.29 9		(5/2+, 7/2, 9/2)	1323.78 4	0.477 12			695.06 15	0.019 7
		1130.25 4	0.139 6			561.22 6	0.073 4			172.5 1	0.059 6
		1097.96 3	0.868 19			328.4 2	0.020 1			564.54 4	0.295 9
		1043.93 3	1.171 25			269.5 4	0.040 2			559.30 3	0.735 18
		941.94 10	0.031 3		(5/2, 7/2)	1295.96 3	0.457 11			461.82 7	0.072 7
		916.79 3	0.470 11			906.55 4	0.30 2			423.61 3	5.43 11
		868.84 5	0.063 6		(3/2, 5/2, 7/2)	1277.49 4	0.134 5			418.37 3	15.74 32
		749.96 5	0.141 4			1272.39 10	0.061 7			381.52 3	52.5 13
		709.13 6	0.054 3			887.90 6	0.050 3			389.37 3	5.59 11
		674.41 4	0.164 6			713.00 12	0.023 3			384.18 4	0.294 8
		577.18 8	0.031 9		(5/2)+	1242.82 4	0.271 7			290.09 3	1.368 25
		354.32 4	0.203 15			1237.56 3	0.755 17			94.12 3	1.41 8
		345.80 8	0.029 10			1200.75 6	0.142 5			42.077 15	9/2+
		153.55 10	0.043 5			853.42 4	0.20 2			5.243 14	3/2-
1916.38 5	(5/2, 7/2)	1916.42	0.010 2			819.23 3	2.80 6				
		1911.12 4	0.112 4			775.77 12	0.021 3				

Table 2. The uncertainties of energies and relative intensities of  $\gamma$ -rays assigned to the decay of  $^{83}\text{Sr}$  but not placed in the decay scheme.

$E_\gamma$ (keV)	758.20 10	856.81 12	1498.60 17	1608.90 18	1709.45 18	1777.90 4	1873.69 4
$I_\gamma$	0.08 3	0.017 3	0.005 2	0.007 2	0.013 2	0.082 4	0.108 5

of  $\beta^+$  decay to the ground state is calculated by subtracting the relative  $\beta^+$  intensity to excited levels from the measured total  $\beta^+$  decay intensity, and the relative ( $\beta^+$ +EC) decay intensity ( $47 \pm 9$ ) to the ground state is also calculated using theoretical  $I_{\beta^+}/I_{\text{EC}}$  value. The renormalization coefficient ( $0.299 \pm 0.015$ ) and ( $\beta^+$ +EC) branching ratio for each level are then obtained.

In summary, in order to study the decay of nuclei with very complex decay scheme, the present paper focuses on the process of analyzing the spectrum, the peak position and fitting interval determined by automatic peak searching code are checked and verified. The nonlinear least square method is adopted to perform curve fitting. Practice proves that manual control of the process of decomposing the complex multiple peaks is effective and necessary. This ensures the accuracy of  $\gamma$ -rays energy and relative intensity and then the deduced level energy is greatly improved.

## Acknowledgments

The project is supported by the National Natural Science Foundation of China under Grant No. 11065001, the Foundation of the Education Department of Jiangxi Province under Grant No. GJJ12372 and the Suranaree University of Technology under contract Nos. 15/2553 and 8/2554. We thank the members of FDS team for their helpful advice and support.

## References

1. X. Yu *et al.*, *Int. J. Mod. Phys. E* **9** (2000) 471.
2. A. Kh. Inoyatov *et al.*, *Eur. Phys. J. A* **50** (2014) 59.