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2 **Vehicle Trajectory Prediction by Knowledge-driven LSTM**

3 **Network in Urban Environments**

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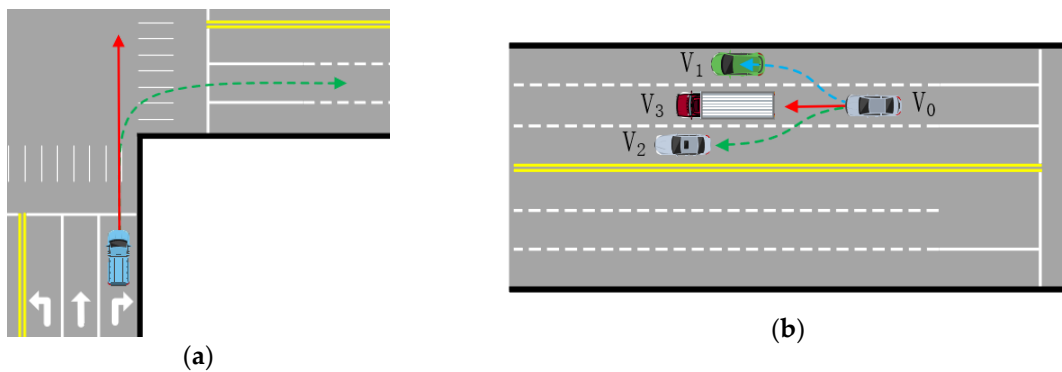
14 **Abstract**

15 An accurate prediction of future trajectories of surrounding vehicles can ensure safe and
16 reasonable interaction between intelligent vehicles and other types of vehicles. Vehicle
17 trajectories are not only constrained by a priori knowledge about road structure, traffic signs,
18 and traffic rules but also affected by posterior knowledge about different driving styles of
19 drivers. The existing prediction models cannot fully combine the prior and posterior knowledge
20 in the driving scene and perform well only in a specific traffic scenario. This paper presents a
21 long short-term memory (LSTM) neural network driven by knowledge. First, a driving
22 knowledge base is constructed to describe the prior knowledge about a driving scenario. Then,
23 the prediction reference baseline (PRB) based on driving knowledge base is determined by
24 using the rule-based online reasoning system. Finally, the future trajectory of the target vehicle
25 is predicted by an LSTM neural network based on the prediction reference baseline, while the
26 predicted trajectory considers both posterior and prior knowledge without increasing the
27 computation complexity. The experimental results show that the proposed trajectory prediction
28 model can adapt to different driving scenarios and predict trajectories with high accuracy due
29 to the unique combination of the prior and posterior knowledge in the driving scene.

30 **1. Introduction**

31 Since the 1980s, autonomous vehicles have been regarded as effective solutions to the
32 problems of road safety, traffic congestion, and energy crisis. However, autonomous vehicles
33 still face many driving difficulties in the real urban traffic environment. A major problem is
34 how to interact safely and reasonably with other types of vehicles in a driving scene.
35 Experienced human drivers can predict the future trajectory of other vehicles in a driving scene,
36 thereby making safe, reasonable, and efficient decisions. Accurately predicting the future
37 trajectory of a vehicle not only can reduce or eliminate the collision risk when autonomous
38 vehicles perform complex driving maneuvers, such as merge, lane change, and overtaking, but

39 also can improve the driving efficiency and comfort of autonomous vehicles [1]. In a real urban
 40 traffic scenario, the vehicle's driving trajectory is not only constrained by prior knowledge,
 41 such as that about the road structure, traffic signs, and traffic rules, but also by uncertain
 42 posterior knowledge, including subjective driving intentions of the driver. The influence of
 43 driving knowledge on vehicle trajectory is shown in Figure 1, where it can be seen that when
 44 the road structure constraints are not considered, the predicted future trajectory, denoted as the
 45 red curve, is incorrect. As shown in Figure 1(b), there is a large slow-moving truck in front
 46 of the target vehicle. In such a case, based on human driving experience, the target vehicle is
 47 likely to adopt a lane change strategy. Therefore, how to fully combine the prior and posterior
 48 knowledge in a driving scene in the prediction process is crucial for accuracy improvement of
 49 the long-term trajectory prediction and safe interaction with other vehicles.



50 Figure 1. Influence of driving knowledge on trajectory prediction: (a) Influence of road structure on trajectory
 51 prediction; (b) Influence of driving experience on trajectory prediction.

52 According to the specific prediction process, the existing prediction models can be roughly
 53 divided into three categories: physics-based models, maneuver-based models, and learning-
 54 based models [2]. The physics-based models use vehicle kinematics and dynamics model to
 55 predict the future position of a target vehicle, and they include the Constant Turn Rate and
 56 Acceleration model [3], Switching Kalman Filters [4], Monte Carlo simulation [5]. However,
 57 these models ignore the prior and posterior knowledge about a driving scenario, such as road
 58 structure, traffic rules, and driver's subjective intentions, which limits these models to short-
 59 term prediction (less than 1 s) [6].

60 Maneuver-based models divide the prediction process into two parts. First, driving intention is
 61 estimated according to the physical state of a vehicle, information about the road network, and
 62 driver behavior, and then the predicted trajectory is fitted based on the driving intention. For
 63 maneuvers classification in more complex scenarios, discriminative learning algorithms,
 64 including the Multi-Layer Perceptions (MLP) [7], Logistic regression [8], Relevance Vector
 65 Machines (RVM) [9], and Support Vector Machines (SVM) [10], have been very popular.
 66 Complex vehicle motion is decomposed into predefined driving action sequences, which makes
 67 driving intention easier to identify and classify, and the prediction result is more stable and
 68 accurate than that of the physics-based models, and the prediction horizon is longer. However,
 69 in complex traffic scenarios, the traditional algorithms, such as finite vector machines and
 70 conditional random fields, have the problem of low scene adaptability, while Bayesian network
 71 and Markov model can solve the problem of driving maneuver classification in uncertain
 72 environments. In addition, the state space of the above models is extremely large, and these
 73 models are prone to "curse of dimensionality", and unable to real-time prediction. Recently,
 74 artificial neural networks have been used to classify vehicle driving actions, but the existing
 75 high-quality calibrated datasets are limited and cannot cover all possible driving scenarios (data

76 sparsity) [11], which makes the network training difficult and challenging, and scene
77 adaptability is low.

78 Learning-based models skip the step of maneuver recognition and perform trajectory prediction
79 directly based on the historical observation of a target vehicle, so the posterior knowledge in
80 driving scenarios can be effectively learned, and incorrect driving motion recognition can be
81 avoided. Recently, artificial neural networks have been used to predict future trajectories of
82 vehicles, bicycles, and pedestrians [12–14]. As a type of recurrent neural network (RNN), the
83 long short-term memory (LSTM) neural network has been proven to be very effective in
84 solving the time series problems, and thus have been widely used in pedestrian trajectory
85 prediction, intersection vehicle destination prediction, and highway vehicle trajectory
86 prediction. However, in previous works, specific-scenario models, such as lane change models
87 for non-intersection sections and left/right turn models for intersection areas, have been
88 proposed [15–17], and the training data needed manual annotation, which increased the training
89 difficulty of the model. In [18], an encoder-decoder LSTM model is proposed for predicting
90 vehicle trajectory by using an occupancy grid map, the maximum prediction horizon of this
91 model is two seconds, which is not sufficient for applications.

92 When an intelligent vehicle is driving in a real urban environment, the driving scene changes
93 dynamically over time, which means that the prediction model should automatically adapt to a
94 driving scene. In order to solve the problem of vehicle adaptability to the driving scene, many
95 studies incorporated the Maneuver-based and Learning-based models. In [19], two LSTMs
96 were used to identify high-level driver intentions and analyze low-level complex vehicle
97 motion dynamics. This method is better geography-adaptive than the traditional LSTM
98 networks. An LSTM model for interaction aware motion prediction of surrounding vehicles on
99 freeways was presented in [20]. This model assigns confidence values to maneuvers being
100 performed by vehicles and outputs a multi-modal distribution over future motion based on
101 these values. The mentioned methods predict the multi-modal trajectory based on maneuver
102 classes, which improves the road adaptability, but the prior knowledge in driving scenarios is
103 not used. In [21], a long short-term memory (LSTM) network was employed to anticipate the
104 driving policy of a vehicle (such as forward, yield, turn left, and turn right) using its sequential
105 history observations. The policy was then used to guide a low-level optimization-based context
106 reasoning process. This method combines the prior knowledge in the driving scene and
107 constructs the cost map to perform the second optimization of the previously obtained driving
108 intention to generate the final predicted trajectory, but the driving intention estimation of the
109 upper-level does not utilize the prior knowledge of the driving scene, and the weight of the
110 function cannot be adjusted adaptively to a driving scenario. Deo and Trivedi [22] adopt a
111 convolutional social pooling LSTM based model. This approach predicts a distribution of
112 future vehicle trajectory dependent on maneuver, but this approach ignores the impact of the
113 interaction of the road users. Dai et al. [23] proposed a Spatio-Temporal LSTM based model,
114 which considers the spatial interactions of the surrounding vehicles, but the constraints of other
115 prior knowledge like road structure, traffic rules and driving experience are not considered.
116 The Dual Learning Model (DLM) which takes information from two different inputs to predict
117 vehicle trajectory was presented in [24]. This model embeds the Occupancy Map and Risk Map
118 into the trajectory model to consider a comprehensive definition of risk in the traffic scene, but
119 the computational complexity usually grows exponentially if the dimensionality of the feature
120 space increases. Thus, it becomes difficult to meet the on-line requirement.

121 In this article, an integrated trajectory prediction model, which combines knowledge reasoning
 122 and LSTM neural networks, is proposed. The contribution of this study can be summarized as
 123 follows:

- 124 1. In order to consider the constraints of the prior knowledge. The Prediction Reference
 125 Baseline obtained by knowledge reasoning is introduced into the LSTM network, where
 126 the proposed model can effectively combine the prior knowledge without increasing the
 127 computation complexity.
- 128 2. In order to learn the spatial interactions of the surrounding vehicles and solve
 129 combinatorial explosion problem caused by a large number of condition attributes. A
 130 method of deterministic scene evaluation is employed to classify and analyze the main
 131 conditions that affect the future trajectory of a vehicle from the perspectives of safety,
 132 legitimacy, and reasonableness, which simplifies modeling of the spatial interactions.
- 133 3. In order to improve the adaptability of the proposed model. The Frenet coordinates based
 134 on the PRB are used to train the LSTM network, and it is not necessary to annotate the
 135 training data set manually according to the specific driving scenario. The results of the
 136 field test prove the adaptive performance of the proposed model.
- 137 4. The performance of the proposed model is evaluated with state-of-the-art methods on a
 138 naturalistic highway driving dataset (NGSIM), the results show that our proposed model
 139 outperforms the state-of-the-art methods.

140 The rest of the paper is organized as follows. The Prediction Reference Baseline determination
 141 method and the proposed LSTM network is presented in Section 2. The proposed prediction
 142 model is evaluated by both simulations and real-traffic urban roadways experiments, and the
 143 obtained results are presented and discussed in Section 3. Finally, the main conclusions,
 144 limitations, and future work are presented in Section 4.

145 2. Materials and Methods

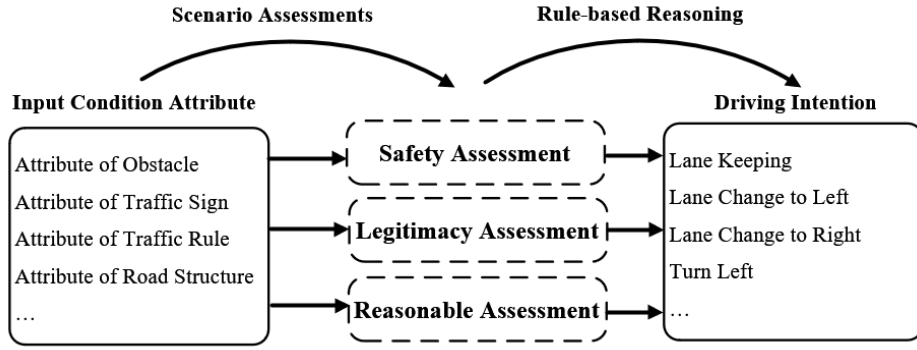
146 2.1. Problem Formulation and Method Overview

147 2.1.1. Problem Formulation

148 The proposed trajectory prediction model is divided into two layers. The first layer determines
 149 the PRB of a target vehicle and the second layer predicts the future trajectory based on the PRB.
 150 PRB is a trajectory that indicates the driving intention of the target vehicle based on prior
 151 driving knowledge, which connect the on-line reasoning system and the LSTM network.

152 The process of driving intention prediction, for a target vehicle V_i at time t is presented in
 153 Figure 2, where it can be seen that it is necessary to understand and evaluate driving scene $S_{v_i}^t$,
 154 and generate the scene evaluation parameters $E_{v_i}^t$ of the target vehicle, including the safety
 155 assessment $SAFE_{v_i}^t$, legitimacy assessment $LEGAL_{v_i}^t$, and reasonable assessment
 156 $REASONABLE_{v_i}^t$, which is expressed as:

$$157 \quad E_{v_i}^t = \{SAFE_{v_i}^t, LEGAL_{v_i}^t, REASONABLE_{v_i}^t\}. \quad (1)$$



158

159

Figure 2. Driving intention prediction process.

160 According to the prior knowledge of driving scenarios, such as traffic rules and driving
 161 experience, the driving intention $b_{v_i}^t$ of the target vehicle is inferred based on the prolog online
 162 reasoning system. A maneuver $b_{v_i}^t$ is classified by the lateral movement of the vehicle, which
 163 is expressed by a finite set \mathcal{B} :

$$164 \quad b_{v_i}^t \in \mathcal{B} := \{LK, LCL, LCR, TR, TL, GS, SS, \dots\}. \quad (2)$$

165 Finite set \mathcal{B} includes the following maneuvers: lane keeping (LK), lane change to left (LCL),
 166 lane change to right (LCR), turn right (TR), turn left (TL), go straight at intersection (GS), stop
 167 before the stop line (SS).

168 Finally, driving intention $b_{v_i}^t$ is fitted to the PRB $PRB_{v_i}^t$ by the cubic Bezier curves.

169 The second layer predicts the future vehicle trajectory. First, the coordinate transformation is
 170 performed on the historical trajectory of the target vehicle based on the PRB $PRB_{v_i}^t$, as shown
 171 in Figure 3. In Figure 3, $s_{v_i}^t$ denotes the distance the target vehicle has traveled along the PRB,
 172 and $l_{v_i}^t$ is the transverse distance between the target vehicle and the $PRB_{v_i}^t$. The absolute
 173 position denoted as $(lat_{v_i}^t, lng_{v_i}^t)$ is transformed to the Frenet coordinates that is denoted as
 174 $(s_{v_i}^t, l_{v_i}^t)$. The set of observations vectors denoted as $O_{v_i}^{t(n)}$ is used for trajectory prediction of
 175 the target vehicle, and it is given by:

$$176 \quad O_{v_i}^{t(n)} = \{s_{v_i}^t, l_{v_i}^t, \kappa_{v_i}^t, \theta_{v_i}^t, v_{v_i}^t, a_{v_i}^t\}, \text{ for } n = t - M + 1, \dots, t, \quad (3)$$

177 where a set $(s_{v_i}^t, l_{v_i}^t)$ denotes the Frenet coordinates, $\kappa_{v_i}^t$ denotes the curvature, $\theta_{v_i}^t$ represents
 178 vehicle heading, $v_{v_i}^t$ denotes the vehicle speed, $a_{v_i}^t$ denotes the vehicle acceleration, and M is
 179 the input step of the network.

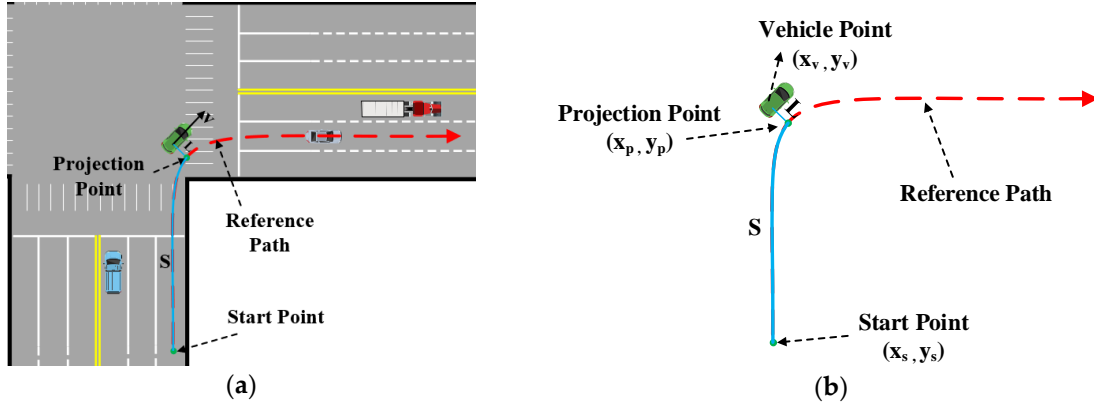
180 The network output $P_{v_i}^{t(n)}$ is expressed as:

$$181 \quad P_{v_i}^{t(n)} = \{s_{v_i}^t, l_{v_i}^t, v_{v_i}^t\}, \text{ for } n = t + 1, t + 2, \dots, t + K, \quad (4)$$

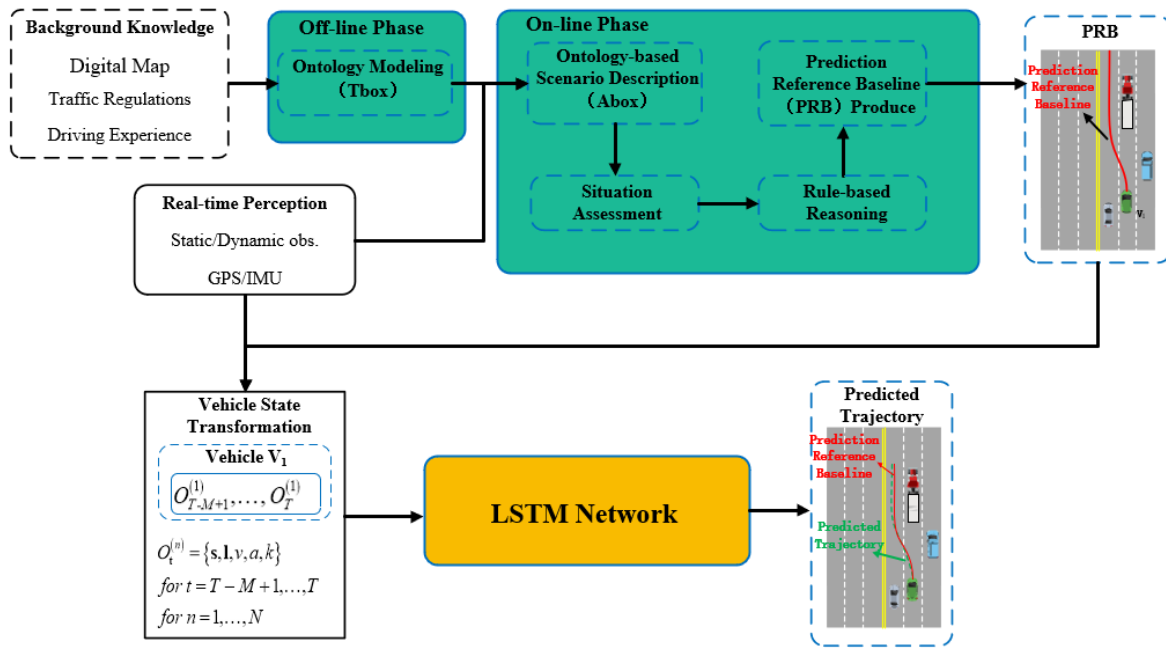
182 where K denotes the output step of the network.

183 Finally, the predicted trajectory denoted as $Tra_{v_i}^{t(n)}$ is obtained by transforming the reference
 184 coordinates to the absolute coordinates represented by the latitude and longitude, which is
 185 expressed as:

$$186 \quad Tra_{v_i}^{t(n)} = \{lat_{v_i}^t, lng_{v_i}^t, v_{v_i}^t\}, \text{ for } n = t + 1, t + 2, \dots, t + K, \quad (5)$$



187 Figure 3. Frenet coordinate of a vehicle: (a) Driving scenario; (b) Description of Frenet coordinate.



188
 189 Figure 4. Overview of the proposed trajectory prediction model.

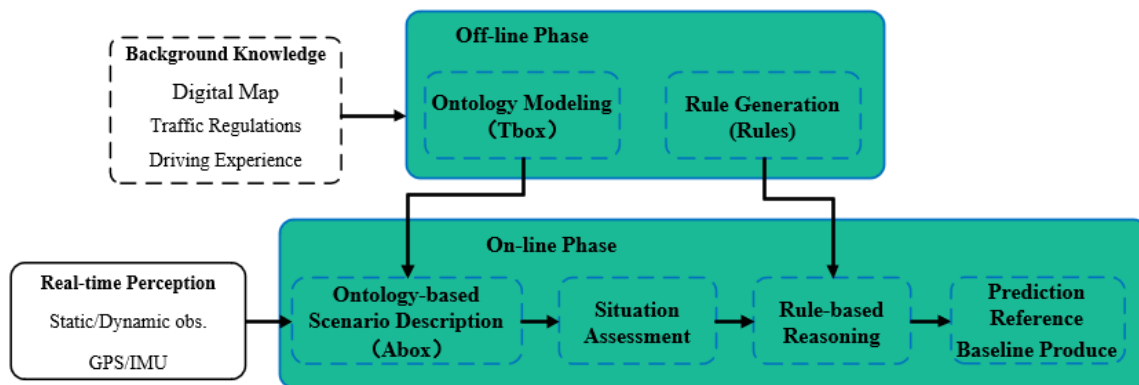
190 2.1.2. Overview of the Proposed Approach

191 This paper proposes a trajectory prediction model based on knowledge reasoning and LSTM
 192 neural network. The architecture of the proposed model is shown in Figure 4, where it can be
 193 seen that the proposed model consists of two phases: PRB determination phase and trajectory
 194 prediction phase. During the PRB determination phase, by analyzing the relationship between
 195 "human-vehicle-road" in the driving scene and extracting the knowledge of road network,
 196 traffic participants, and road traffic facilities, the conceptual ontology model of the driving
 197 scene is established. The main conditional attributes that affect the behavior decision-making
 198 process are classified and analyzed from the perspectives of safety, legitimacy, and

199 reasonableness using the proposed deterministic situation assessment method, and situation
 200 parameters in the horizontal and vertical directions are obtained. The behavior prediction rule
 201 base is constructed using the situation parameters, traffic rules, and driving experience. Based
 202 on the prolog online reasoning system, the behavioral prediction rules are matched with the
 203 factual knowledge obtained by the conceptual ontology model, and the driving intentions are
 204 inferred. Finally, a third-order Bezier curve is used to fit the driving intention to a PRB. The
 205 trajectory prediction phase uses the LSTM network to learn the continuous features of the
 206 historical trajectory of a target vehicle on the basis of the PRB and generates the final predicted
 207 trajectory.

208 2.2. Prediction Reference Baseline Determination

209 The architecture of the proposed PRB Determination method is presented in Figure 5, where it
 210 can be seen that this method consists of online and offline phases. The offline phase establishes
 211 the conceptual ontology model (TBOX) of a driving scene and extracts the behavioral
 212 prediction rules based on traffic rules and driving experience. According to the conceptual
 213 ontology model, the road network and real-time environment perception information are used
 214 to instantiate the entities and related relationships in the driving scene (ABOX). The entities
 215 and entity relationships in the driving scene are classified by the deterministic scene assessment
 216 method and analyzed from the perspectives of safety, legitimacy, and reasonableness. The
 217 scene evaluation parameters in both horizontal and vertical directions are generated, and the
 218 behavioral prediction rules are matched with the scene evaluation parameters by using the
 219 prolog online reasoning system. The driving intentions are inferred, and finally, the third-order
 220 Bézier curve is used to fit the driving intention to the PRB.

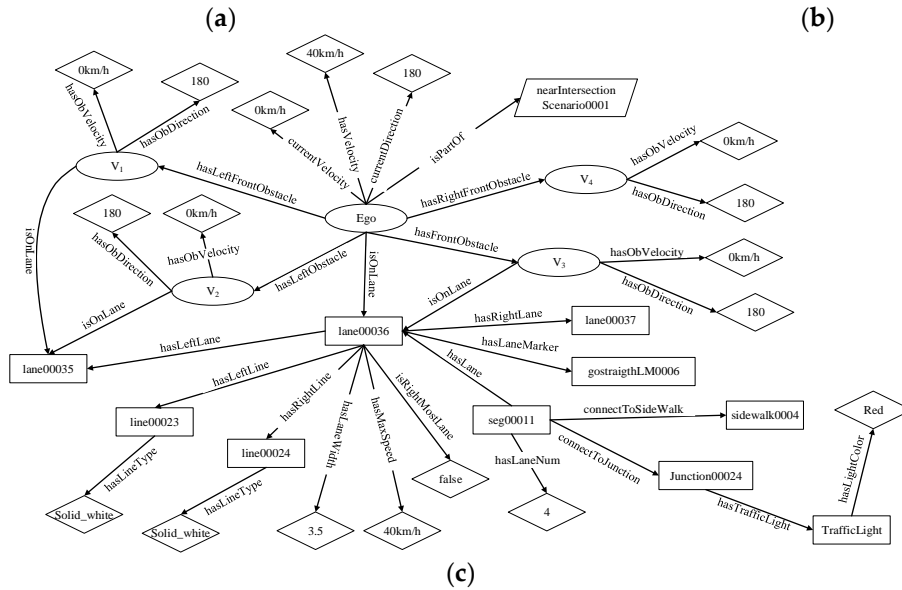
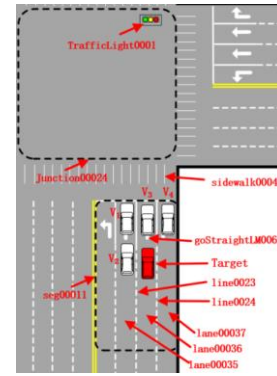


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222

Figure 5. The architecture of the proposed Prediction Reference Baseline Determination method.

223 2.2.1. Semantic Modeling of Driving Scene

224 In a driving scenario, there are various road element entities, such as traffic participants, road
 225 networks, and road traffic facilities in urban driving scenarios. The environment perception
 226 system can provide only the spatial location of each entity, but it cannot describe the correlation
 227 between entities, and make full use of prior information, such as traffic rules and driving
 228 experience, which is crucial for improving the prediction model adaptability to the driving
 229 scene. Ontology, as a form of knowledge expression, is used to model the concepts of specific
 230 domains and relationships between concepts, which can be used to model driving scenarios
 231 effectively [25–27].



232 Figure 6. Scene modeling: (a) Real traffic scenario; (b) Concrete driving scene; (c) Semantic description of the
 233 concrete scene.

234 The conceptual ontology model is divided into two module types: entities and attributes. This
 235 study takes the target vehicle as a perspective and summarizes five entity types on the basis of
 236 [28]:

237 1) Target Vehicle

238 The target vehicle entity describes the vehicle to be predicted.

239 2) Behavior

240 The behavior entity is a collection of driving maneuvers of a vehicle. Three behavior types are
 241 designed: LongtiBehavior, LatiBehavior, and AdvancedBehavior. The LongtiBehavior
 242 represents basic vertical driving behavior and includes four behaviors: accelerate, decelerate,
 243 keep, and stop. The LatiBehavior represents basic horizontal driving behavior and includes
 244 three behaviors: ChangeToLeft, ChangeToRight, and KeepLane. The AdvancedBehavior
 245 represents advanced driving behavior and includes two behaviors: Overtake and Merge.

246 3) Obstacle

247 The obstacle entity represents a collection of obstacle entities encountered by a vehicle during
 248 driving. This work divides obstacles according to the behavior characteristics of obstacle
 249 entities in driving scenarios into two categories: StaticObstacle and DynamicObstacle.

250 4) Road network

251 The road network entity represents the topological connection of roads by intersecting points
 252 and lines. RoadType includes different road types. RoadPart describes the components of the
 253 road network and is divided into AreaEntities and PointEntities. AreaEntities refer to road
 254 entities that can be abstracted into lines and areas, such as lane, side walk, junction, and
 255 segment, while PointEntities refers to road entities that can be abstracted into points, such as
 256 road signs, traffic signs, and traffic lights.

257 5) Driving Scenario

258 The driving scene entity refers to a collection of road entity elements encountered when a
 259 vehicle travels in different road areas. In this work, driving scenarios are divided into three
 260 categories: InSpecialAreascenario (special area driving scenario), OnRoadscenario (road
 261 driving scenario), and NearSpecialAreascenario (near special region driving scenario).
 262 InSpecialAreascenario category can be further divided into IntersectionScenario (intersection
 263 scene), TunnelScenario (tunnel scene), BridgeScenario (elevated scene), and UturnScenario
 264 (UTurn scene).

265 The object attribute is used to describe the relationship between concept classes. This attribute
 266 restricts the described relationship regarding the domain and range. The data attribute restricts
 267 the described relationship through the definition and value domains. The definition domain is
 268 a class type.

269 The described ontology modeling process of driving scenario is equivalent to filling the
 270 background knowledge of the TBox that constitutes the ontology knowledge base, but the
 271 situational knowledge in the ABox is still lacking. According to the road elements of a real
 272 driving scenario, the driving scenario needs to be re-expressed using the conceptual model of
 273 the TBox, which is an instantiation of the ontology model. A real traffic scenario is displayed
 274 in Figure 6(a); a concrete driving scene that includes instances of defined classes is presented
 275 in Figure 6(b), and its semantic description is presented in Figure 6(c). The instances of
 276 RoadNetwork are added to the ABox as prior knowledge, and instances of the obstacle are
 277 asserted in real time.

278 2.2.2. Situation Assessment

279 After obtaining a semantic description of a driving scene, it is necessary to determine and
 280 evaluate condition attributes that affect the driving intention in the driving scene, so as to
 281 estimate the driving intention of a target vehicle. In order to solve the problem of combinatorial
 282 explosion due to numerous condition attributes [29], a deterministic scenario assessment
 283 method is adopted to classify and analyze the key attributes that affect driving intentions from
 284 the perspectives of safety, legitimacy, and reasonableness.

285 Deterministic scenario assessment methods use the threat assessment indicators: TTC (time to
 286 collision), THW (time headway), TTB (time to brake), DST (deceleration to safety time), and
 287 MSM (minimal safety margin) in rule-based systems, and the probability of collision is

288 estimated as a binary value. For instance, Glaser et al. [30] used the TTC and TIV (time
 289 intervehicles) indicators to evaluate the possibility of collision. Samyeul et al. [31] proposed a
 290 distributed reasoning method by dividing the current and adjacent lanes into the front and rear
 291 areas, and the TTB and MSM indicators were used to evaluate the possibility of collision in
 292 the front area, while the TTC and MSM indicators were used to evaluate the collision of rear
 293 area collision possibility.

294 The proposed deterministic scenario assessment method consists of two parts. First, the driving
 295 scenario is determined by querying the knowledge base with the current vehicle position. Then,
 296 a reasoning structure of an obstacle is constructed in eight regions of interest to make safety
 297 assessment, and a binary result (safe or dangerous) is calculated for each region using critical
 298 indicators TTC and TIV. Finally, legitimacy and reasonableness assessments are made to
 299 predict the maneuver of the target vehicle.

300 1) Safety assessment

301 Safety primarily refers to whether the surrounding obstacles pose a threat to a vehicle,
 302 especially in the area ahead, but it also refers to whether the left or right lane can provide a safe
 303 lane change. This paper constructs the eight-direction obstacle inference model. For each area,
 304 the TTC and TIV indicators are used for safety assessment. The TTC indicator is defined as a
 305 time when two vehicles continue to collide on the same trajectory at the current speed, and it
 306 is defined by:

$$307 \quad TTC = \frac{D_i}{v-v_i}, \quad (6)$$

308 where D_i denotes the relative distance between the following vehicle and followed vehicle, V
 309 denotes the speed of the following vehicle, and V_i is the speed of followed vehicle.

310 The threshold value TTC_{th} is used to judge whether a vehicle is dangerous in high-speed
 311 scenarios. The risk assessment formula is as follows:

$$312 \quad R_{TTC}(t) = \begin{cases} 0, & t \geq TTC_{th} \\ 1, & t < TTC_{th} \end{cases}. \quad (7)$$

313 when the calculated collision time t between the following vehicle and followed vehicle is
 314 greater than TTC_{th} , the current scene is considered to be safe; otherwise, it is considered to be
 315 dangerous.

316 The TIV indicator is used to detect low-speed difference scenarios. When the speeds of two
 317 vehicles are similar in value, the TIV indicator is used to judge the degree of danger, and it is
 318 calculated by:

$$319 \quad TIV = \frac{D_i}{v}. \quad (8)$$

320 threshold TIV_{th} is used to distinguish between safe and dangerous scenes in low workshop
 321 distance scenes. The TIV risk assessment formula is as follows:

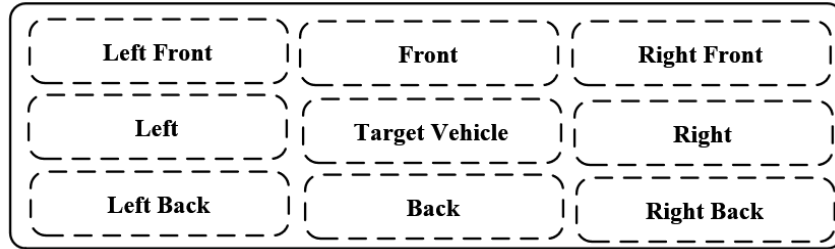
$$322 \quad R_{TIV}(t) = \begin{cases} 0, & t \geq TIV_{th} \\ 1, & t < TIV_{th} \end{cases}. \quad (9)$$

323 when the calculated vehicle interval time t between the following vehicle and followed vehicle
 324 is greater than TIV_{th} , the current scene is considered to be safe; otherwise, it is considered to
 325 be dangerous, and in that case, the following car needs to perform a certain action to avoid a
 326 possible collision.

327 In each region, only when $R_{TTC}(t)$ and $R_{TIV}(t)$ are calculated safety synchronously, the
 328 region is considered to be safe. The risk assessment of an region is determined as:

$$329 \quad r_{Region}(t) = \begin{cases} 1, & R_{TTC}^{Region}(t) + R_{TIV}^{Region}(t) \geq 1 \\ 0, & \text{otherwise} \end{cases}, \quad (10)$$

330 where *Region* represents one of the eight regions, as shown in Figure 7; when $r_{Region}(t)$ has
 331 a value of zero, the area is considered to be safe; and, when $r_{Region}(t)$ has a value of one, the
 332 area is considered to be dangerous.



333

334

Figure 7. Example individuals in traffic scenario.

335 The degree of danger in the area ahead is calculated by:

$$336 \quad r_F(t) = \begin{cases} 1, & R_{TTC}^F(t) + R_{TIV}^F(t) \geq 1 \\ 0, & \text{otherwise} \end{cases}, \quad (11)$$

337 when the calculated values of the TTC and TIV indicators in the current area are greater than
 338 the predefined threshold, the following result message is obtained: safeToGo (targetVehicle,
 339 keep); when the calculated values of TTC and TIV indicators in the current area are both less
 340 than the predefined deceleration threshold, but greater than the corresponding parking
 341 threshold, the result message is: safeToGo (targetVehicle, dec), and in this case, a lane change
 342 can be performed to improve driving efficiency; otherwise, the result message is: safeToGo
 343 (targetVehicle, stop).

344 The safety assessment of adjacent lanes is conducted using the same assessment formula as
 345 that of the area ahead. If the left lane is taken as an example, then the degree of danger is
 346 expressed as:

$$347 \quad r_L(t) = \begin{cases} 1, & \text{has left vehicle at time } t \\ 0, & \text{otherwise} \end{cases}, \quad (12)$$

348 when there are vehicles in the left area, the left lane can be considered to be dangerous;
 349 otherwise, the safety of the left front and left rear areas are respectively evaluated by:

$$350 \quad r_{FL}(t) = \begin{cases} 1, & R_{TTC}^{FL}(t) + R_{TIV}^{FL}(t) \geq 1 \\ 0, & \text{otherwise} \end{cases}, \quad (13)$$

$$351 \quad r_{BL}(t) = \begin{cases} 1, & R_{TTC}^{BL}(t) + R_{TIV}^{BL}(t) \geq 1 \\ 0, & \text{otherwise} \end{cases}, \quad (14)$$

352 Therefore, the safety assessment of the left lane is as follows:

$$353 \quad Risk_L(t) = \begin{cases} 1, & r_L(t) = 1 \text{ or } r_{FL}(t) + r_{BL}(t) \geq 1 \\ 0, & \text{otherwise} \end{cases} \quad (15)$$

354 If the left lane is safe, safeToLeft (targetVehicle, true) will be generated; otherwise, the
355 scene evaluation parameters will be instantiated as safeToLeft (targetVehicle, false).

356 2) Legitimacy assessment

357 The legality assessment includes three assumptions. First, when a vehicle is driving on the road,
358 it cannot exceed the maximum speed limit of the road; second, when the vehicle is driving to
359 the pre-intersection, it is necessary to pay attention to the change in traffic lights and obey the
360 traffic rules; third, when a vehicle is about to change the lane, the adjacent lane should allow
361 lane changes.

362 3) Reasonableness assessment

363 Reasonableness assessment generally refers to whether lane changing and other driving
364 behaviors affect the current goal of a target vehicle. Based on the current lane of the target
365 vehicle, the specific road section or lane to be driven can be known. For instance, on the one
366 hand, if the next area to be driven by the target vehicle is an intersection, and the distance
367 between the target vehicle and the stop line is less than δ , then lane change is not recommended.
368 On the other hand, if the distance between the target vehicle and the stop line is greater than δ ,
369 lane change can be performed. Reasonableness assessment introduces a situation parameter set
370 (*reasonableToLeft*, *reasonableToRight*), which is defined as data properties in the
371 ontology model.

372 2.2.3. Rule-Based Reasoning

373 The driving intention is determined based on traffic rules and driving experience, where the
374 traffic rules are mainly used to limit the driving behavior while the driving experience is
375 utilized to summarize the understanding and cognition of human drivers in different scenes and
376 obtain some rules that are not specific traffic rules but are conducive to the reasonable driving.
377 According to the different driving scenarios defined in the driving knowledge base, the rules
378 stored in the driving knowledge base are divided into several categories. Different scenarios
379 have different key road entities. For instance, unlike OnRoadScenario, in
380 NearIntersectionScenario, traffic lights are considered. Also, the classification of traffic rules
381 can reduce the rule search space and reasoning time.

382 In order to save computing resources and reduce reasoning time, SWI-Prolog language is used
383 to write rule knowledge, which is represented as a set of driving scene-driving behavior
384 mapping pairs, where driving behavior is described as a rule head, and the driving scene is
385 described as a rule body. On the basis of [28], this paper adds the scene assessment as an

386 intermediate link of mapping driving scene to the driving behavior and reorganizes 57 rules.
387 Some of the prediction rules are presented in Table 1.

388 The online reasoning process can be described as follows. First, the real-time facts related to
389 the scene are used as input, and each rule statement is matched. If all the facts of the
390 corresponding rule are matched, the matched prediction result will be obtained, and the next
391 rule statement will be matched until each rule is matched. When all matched results are
392 obtained, the final result denotes the predicted driving intention.

393 Table 1. Prediction rules used in this study.

ID	SWRL Rules
Rule #1	TargetVehicle(target), currentRoadState(target,"ApprJunction"), isOnSegment(target,Seg), connectToJunction(Seg,Junc), intersection(Junc), hasTrafficLight(Junc,TL), (hasLightColor(TL,"red"); hasLightColor(TL,"yellow")), connectToStopLine(Seg,SL), distToStopLine(SL,DL), DL < 10.
	legalToGo(target,SS)
Rule #2	TargetVehicle(target), currentRoadState(target,"ApprJunction"), isOnSegment(target,Seg), connectToJunction(Seg,Junc), intersection(Junc), hasTrafficLight(Junc,TL), hasLightColor(TL,"green"), connectToStopLine(Seg,SL), distToStopLine(SL,DL), DL =< 20.
	LegalToGo(target,acc)
Rule #3	TargetVehicle(target), currentVelocity(target,V), hasFrontObstacle(target,FO), distToObstacle(FO,DF), (DF/V) < 3, (DF/V) >= 2.
	SafeToGo(target,dec)

394 2.2.3. Prediction Reference Baseline Fitting

395 After obtaining the driving intention of the target vehicle, the driving intention is converted
396 into the Prediction Reference Baseline using the cubic Bezier curves. As shown in Figure 8,
397 first, a target lane is selected based on the driving intention and road network, where p_0
398 represents the current position of the target vehicle, and p_3 is selected from the centerline of
399 the target lane with distance L_d from p_0 , and L_d is obtained based on the driving experience.
400 The Prediction Reference Baseline is divided into three parts by p_0 and p_3 : the predicted
401 extension, the historical extension, and the intention segment. In addition, L_p and L_h are
402 determined by the input and output steps of the LSTM neural network.

403 As shown in Figure 8(c), the cubic Bezier curve constructed by four control points is used to
404 generate the intention segment, which is expressed as:

$$405 \quad C(t) = B_{0,3}(t)P_0 + B_{1,3}(t)P_1 + B_{2,3}(t)P_2 + B_{3,3}(t)P_3, \quad (16)$$

406 where $B_{i,3}$ is the Bernstein polynomial and it is given by:

$$407 \quad B_{i,3}(t) = \binom{3}{i} \left(\frac{t_1-t}{t_1-t_0} \right)^{3-i} \left(\frac{t-t_0}{t_1-t_0} \right)^i, t \in \langle 0,1,2,3 \rangle. \quad (17)$$

408 The coordinate system (X'', Y'') is built with the origin P_0 at the vehicle center. The x-axis
409 direction is the vehicle's initial heading, the terminal state will be the end point P_3 , and P_1 and

410 P_2 are obtained by moving forward for distance d along the vehicle's initial heading direction
 411 from the start point and backward for distance d along the terminal heading from the end
 412 point P_3 , respectively. The position of the control points in the above coordinate system is
 413 expressed as:

$$414 \quad P_0 = \begin{bmatrix} 0 \\ 0 \end{bmatrix}, P_1 = \begin{bmatrix} d \\ 0 \end{bmatrix}, P_2 = \begin{bmatrix} L_x - d \cos \omega \\ L_y - d \sin \omega \end{bmatrix}, P_3 = \begin{bmatrix} L_x \\ L_y \end{bmatrix}, \quad (18)$$

415 where L_x and L_y are lateral and longitudinal offsets of the terminal state P_3 to P_0 , respectively;
 416 ω is the angle between the terminal heading and the direction of the x-axis. The terminal
 417 heading is defined as the tangential direction of the closest point on the reference path to P_3 .

418 Equation (16) and (17) can be rewritten by applying (18), so the Bezier curve can be
 419 represented as:

$$420 \quad x(t) = (3d + 3d \cos \omega - 2L_x)t^3 - 3(2d + d \cos \omega - L_x)t^2 + 3dt, \quad (19)$$

$$421 \quad y(t) = (3d \sin \omega - 2L_y)t^3 - 3(d \sin \omega - L_y)t^2. \quad (20)$$

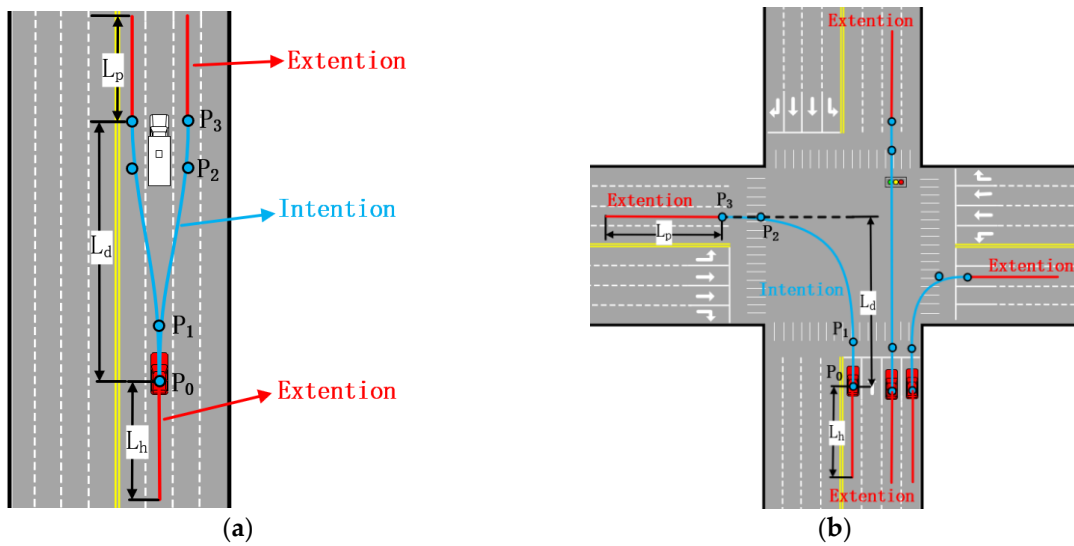
422 Besides, the curvature of the generated path can be derived by applying (20) and (21), which
 423 leads to:

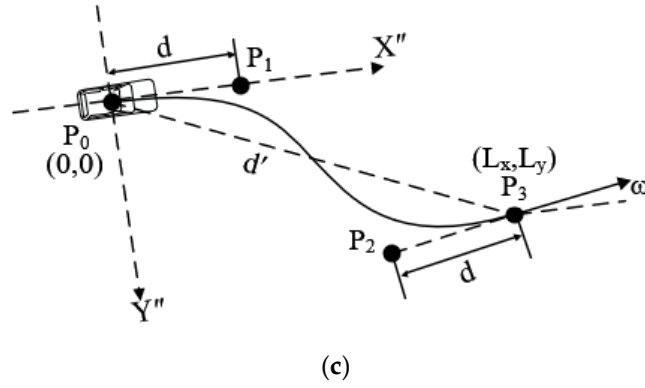
$$424 \quad \kappa(t) = \frac{x'(t)y''(t) - y'(t)x''(t)}{(x'(t)^2 + y'(t)^2)^{3/2}}, \quad (21)$$

425 The maximum of the curvature should satisfy the condition given by equation (22) to meet the
 426 vehicle's nonholonomic constraint.

$$427 \quad \kappa(t_m) \leq \frac{\tan(\varphi_{max})}{L} \quad (22)$$

428 In equation (22), L denotes the vehicle wheelbase, and φ_{max} denotes the maximum steering
 429 angle of the vehicle.





430 Figure 8. Schematic diagram of Prediction Reference Baseline fitting: (a) Lane-changing scene; (b) Intersection
431 turning scene; (c) The cubic Bezier curves.

432 The maximum of the curvature $\kappa(t_m)$ is a function of d . The suitable value of d that satisfies
433 the vehicle's nonholonomic constraint can be found by brutal searching from $\frac{d'}{6}$ to $\frac{d'}{2}$, where
434 d' denotes the distance between P_0 and P_3 . The processing time can be reduced by building a
435 look-up table that matches a given set with the corresponding maximum curvature of the Bezier
436 curve.

437 2.3. LSTM Network Driven by Knowledge

438 Since different drivers have different driving styles, in order to accurately predict the future
439 trajectory of a vehicle, in this work, an LSTM neural network is employed to learn the
440 continuous features of the historical trajectory. The LSTM is an RNN type that can effectively
441 overcome the problem of gradient disappearance [32]. The LSTM is composed of a unit
442 memory that stores the previous input sequence information and a gating mechanism that
443 controls the information flow between input, output, and unit memory. There are three gates in
444 the core design of the LSTM network, namely the input gate, the forget gate, and the output
445 gate. The specific network structure is shown in Figure 9. The forget gate is used to control
446 how much information in c_{t-1} is retained in c_t . The input gate determines how much
447 information of x_t remains in c_t , and finally, the output gate determines how much information
448 in the output o_t is output to h_t by the control unit c_t . The work of the LSTM is described by
449 the following recursive equations:

$$450 \quad f_t = \sigma(W_f \cdot [h_{t-1}, x_t] + b_f), \quad (23)$$

$$451 \quad i_t = \sigma(W_i \cdot [h_{t-1}, x_t] + b_i), \quad (24)$$

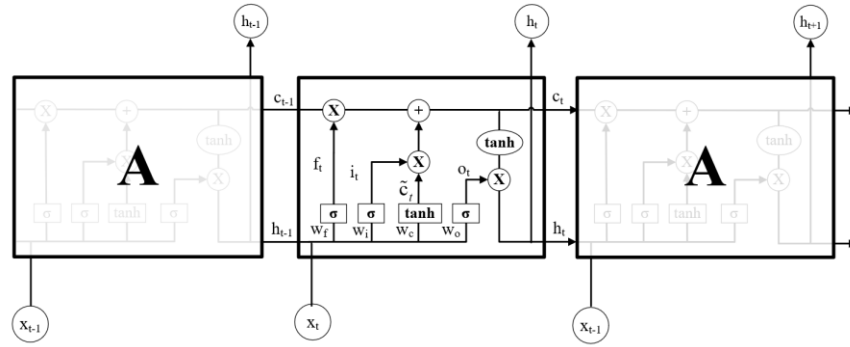
$$452 \quad \tilde{c}_t = \tan h(W_c \cdot [h_{t-1}, x_t] + b_c), \quad (25)$$

$$453 \quad c_t = f_t \odot c_{t-1} + i_t \odot \tilde{c}_t, \quad (26)$$

$$454 \quad o_t = \sigma(W_o \cdot [h_{t-1}, x_t] + b_o), \quad (27)$$

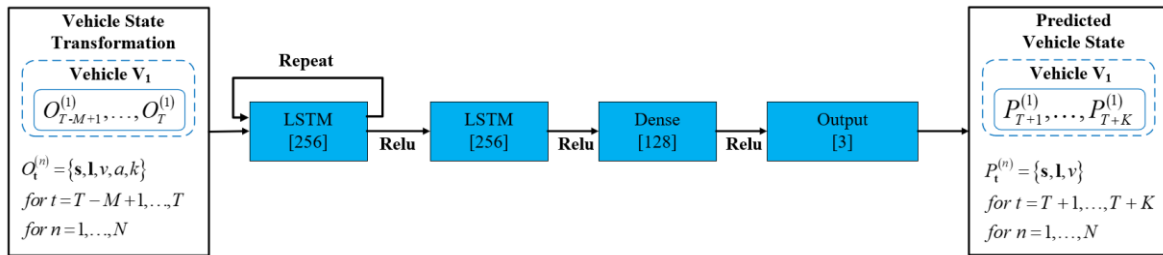
$$455 \quad h_t = o_t \odot \tan h(c_t), \quad (28)$$

456 where x_t denotes the input vector, $\sigma(x)$ denotes the activation function, W denotes the linear
457 transformation matrix, b denotes the offset vector; i_t , f_t , and \tilde{c}_t are gate vectors, c_t
458 represents the amount of cell memory, and lastly, h_t denotes the output.



459

Figure 9. The internal structure of an LSTM cell.



460

Figure 10. Network structure used as a reference design.

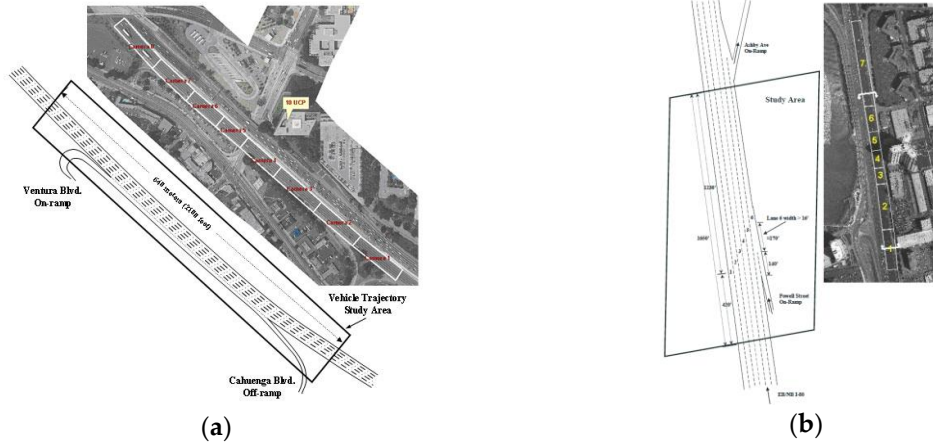
461 In this work, the network presented in Figure 10 is used as a reference structure. This network
 462 has two layers consisting of 256 LSTM cells, followed by one time-distributed layer consisting
 463 of 128 neurons, and the final dense output layer containing as many cells as the number of
 464 outputs. The network input is a tensor of track histories of a vehicle. The network output
 465 consists of the future coordinates and velocity of the vehicle. Since the prior knowledge about
 466 the driving scene is expressed by a priori reference trajectory, the network can learn the
 467 posterior knowledge about the driving scene only from the relative relationship between the
 468 historical trajectory and the prior reference trajectory. Compared with the existing prediction
 469 models based on the LSTM network, the proposed prediction model reduces the network
 470 training difficulty and decreases demand for the computing performance of the vehicle
 471 platform.

472 3. Results and Discussion

473 3.1. Data Preparation and Model Training

474 3.1.1. The training dataset

475 The Next Generation Simulation (NGSIM) dataset in I-80 and US101 sections are used for
 476 model training and testing [33], this dataset is derived from the US Federal Highway
 477 Administration, which is currently the largest public natural driving public data source, and
 478 thus has been widely used in the literature [34,35]. The layouts and top-down views of the
 479 US101 AND I-80 sections are shown in Figure 11. Each data frame includes many vehicle's
 480 parameters, including the position, velocity, yaw rate, size, and others. The sampling frequency
 481 of the dataset is 10 Hz; therefore, in this work, Δt is set to 0.1 s.



482 Figure 11. Layouts and top-down views of the sites used for the collection of the NGSIM: (a) US101; (b) I80.

483 3.1.2. Data Preparation

484 The vehicle positioning data in the NGSIM dataset are obtained by video analysis, so the
 485 recorded trajectory contains a lot of noise [27]. Therefore, the vehicle kinematics model and
 486 the road geometric are used to filter the original data, which is expressed as:

$$487 \quad 0 < \kappa_i < \kappa_{max}, \quad (29)$$

$$488 \quad \theta_{min} < \theta < \theta_{max}, \quad (30)$$

$$489 \quad \theta_{r_i} > \theta_{rate}, \quad (31)$$

$$490 \quad \theta_{r_i} = \frac{(\theta_{i+1} - \theta_i)}{t_2 - t_1}. \quad (32)$$



491 Figure 12. Extraction of the lane's centerline: (a) Extraction results obtained by Google Earth; (b) Shapefile of
 492 the US101 highways.

493 The vehicle position is transformed to the Frenet coordinates based on the centerline. As shown
 494 in Figure 12(b), the centerline of each lane is extracted and fitted using the shapefile, and the
 495 centerline that the target vehicle was initially driven is selected as a reference baseline. For
 496 each original coordinate point (x_v, y_v) , the corresponding mapping point (x_p, y_p) on the
 497 reference baseline is determined, and the Frenet coordinates (s_v, l_v) are obtained by:

$$l_v = \sqrt{(x_p - x_v)^2 + (y_p - y_v)^2}, \quad (33)$$

$$s_v = S(x_p, y_p), \quad (34)$$

where l_v denotes the Euclidean distance between (x_v, y_v) and (x_p, y_p) , $S(x_p, y_p)$ denotes the length from the mapping point (x_p, y_p) to the starting point of the reference trajectory.

In addition, four other features: curvature κ , velocity V , acceleration \mathbf{a} , and heading θ , are also selected so as to compose the observation vector \mathbf{o} with the Frenet coordinates (s, l) .

3.1.3. Training Details

There were 8311 filtered trajectories; 80% of the trajectories were selected as the training set, 10% as the test set, and the remaining 10% was used as the verification set to observe if the model is over-fitted.

The network was trained using mini-batches with a size of 64. Due to the limitation on a sensor measurement range and noise in practical application scenarios, it was difficult to track dynamic vehicles stably for a long time, so the network was trained using windows that consisted of 30 inputs, representing a total of 3s past observations. The ADAM optimizer was used; the learning rate was 0.0005 and ReLU activation with $\alpha = 0.1$. The loss function adopted the MSE (mean square error) between the predicted sequence and the ground truth sequence; the code used to generate the model was written in Keras, and the training was performed on GPU using the TensorFlow backend with a batch size of 32; the model training contained 16 epochs.

3.2. Testing Results and Discussion

3.2.1. The Impact of the Prediction Reference Baseline

To investigate the impact of considering Prediction Reference Baseline on the accuracy of the proposed method. The RMSE performance of the proposed model is present with three modifications.

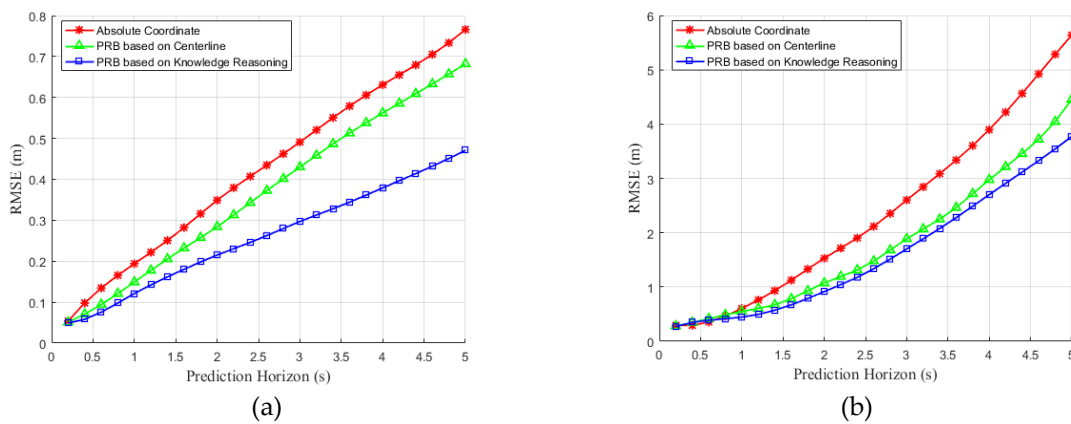


Figure 13. Effectiveness of considering Prediction Reference Baseline in the vehicle trajectory prediction: (a) Lateral position error; (b) Longitudinal position error.

524 In one experiment, the system is trained and tested with the absolute coordinate, in the second,
 525 the centerline that the target vehicle was initially driven is selected as a PRB, and finally in the
 526 third experiment, the PRB of the target vehicle is determined by the method in Section 2, while
 527 the other attributes of the three model are unchanged. Figure 13 shows the accuracy of the
 528 trajectory prediction for different time horizons, the RMSE value of the model is decreased by
 529 adding the PRB for both lateral and longitudinal trajectory.

530 3.2.2. Comparative study

531 To evaluate the proposed approach, we pursue a direct comparison with state-of-the-art vehicle
 532 trajectory prediction using the same dataset (i.e., NGSIM). The results show that the proposed
 533 method outperforms the state-of-the-art model and decreases the overall RMSE value of the
 534 system by 10 percent on average. Table 2, summarizes the RMSE values comparing the
 535 proposed methods with the baseline trajectory prediction models in the literature [20], [22],
 536 [23], [24], [36].

537 The comparison results show that the proposed Knowledge-driven LSTM Network has better
 538 performance in RMSE for NGSIM. Note that as compared to the baseline [24], the prediction
 539 accuracy gets a slight improvement, but the proposed method enhances the real-time
 540 performance and much reduces the computational complexity due to the reduction of the
 541 feature space dimension.

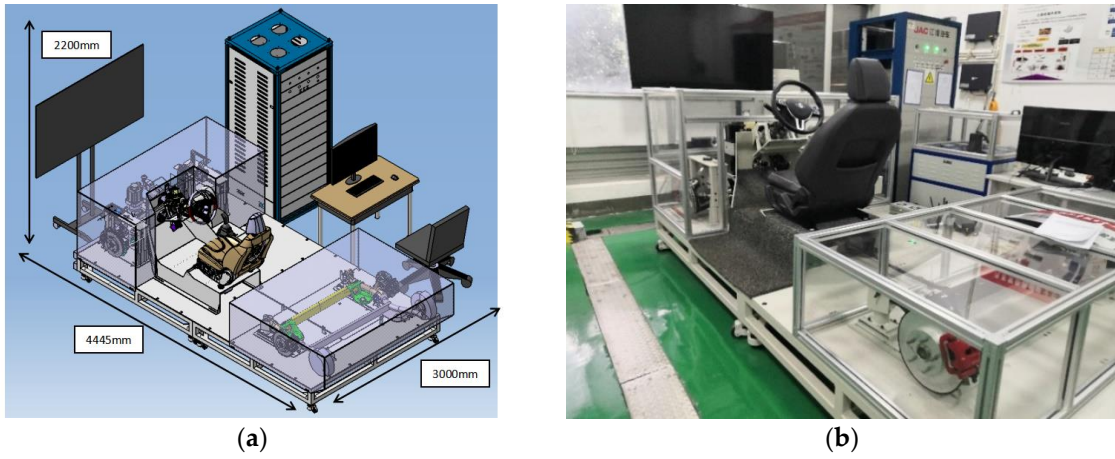
542 Table 2. RMSE comparison of the proposed method with the baseline models and state-of-the-art.

Prediction Horizon (s)	M-LSTM [20]	CS-LSTM [22]	NLS-LSTM [36]	ST-LSTM [23]	DLM [24]	Proposed method
1	0.58	0.61	0.56	0.58	0.41	0.41
2	1.26	1.27	1.22	1.21	0.95	0.89
3	2.12	2.09	2.02	1.97	1.72	1.64
4	3.24	3.10	3.03	2.85	2.64	2.47
5	4.66	4.37	4.30	3.89	3.87	3.68

543 3.3. Simulation Results and Discussion

544 3.3.1. Simulation Experimental Platform

545 The simulation experiments were based on the JAC's automatic driving hardware-in-the-loop
 546 test platform. The experimental simulation platform is presented in Figure 13, where it can be
 547 seen that the experimental platform included the real vehicle braking system, steering system,
 548 sensor system, and network communication system, which had dSPACE (Matlab/Simulink) as
 549 a core. The controller rapid prototyping platform was built, virtual reality interfaces and
 550 environment-aware sensor modules were provided using the PreScan software, and the CarSim
 551 software was used to run the vehicle dynamic model and provide a platform that could be
 552 quickly verified for automatic driving algorithm testing.



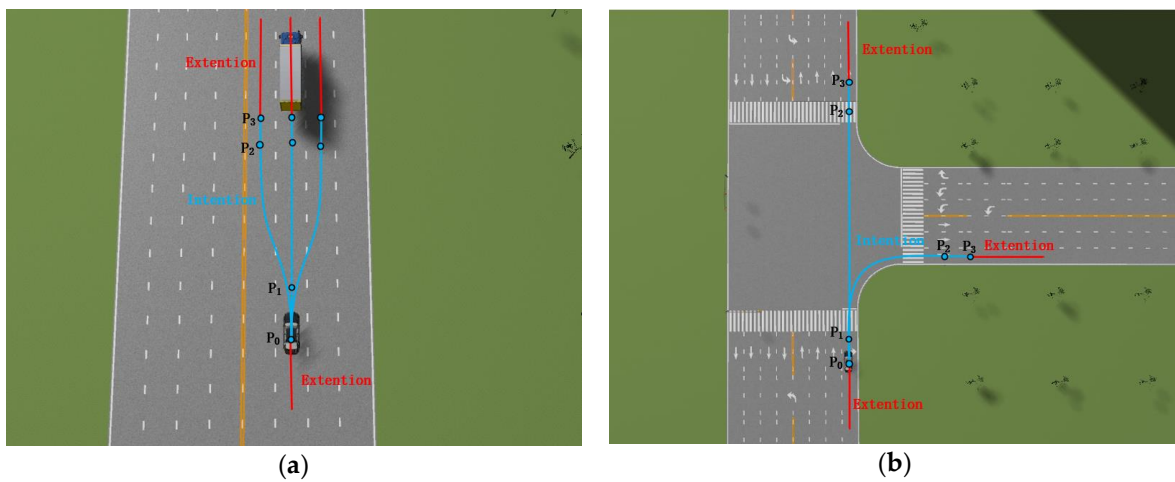
553 Figure 14. Experimental simulation platform: (a) Design of the simulation platform; (b) Photo of the simulation
 554 platform.

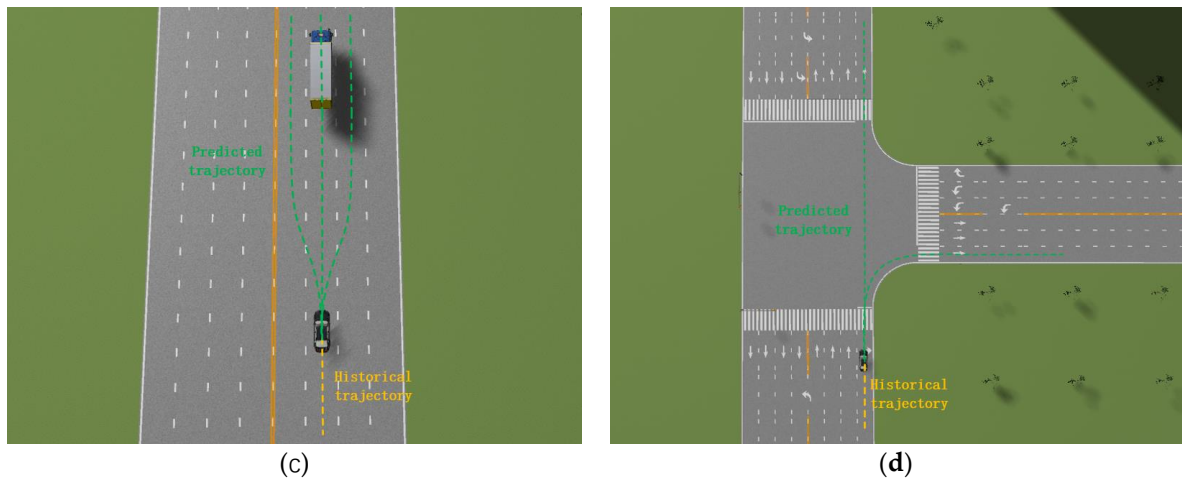
555



556 Figure 15. Simulation scenario layout.

557





558 Figure 16. Simulation results: (a) On the road scenario; (b) Intersection scenario. (c) Simulation results of the on
 559 the road scenario; (d) Simulation results of the intersection scenario.

560 3.3.2. Simulation Results

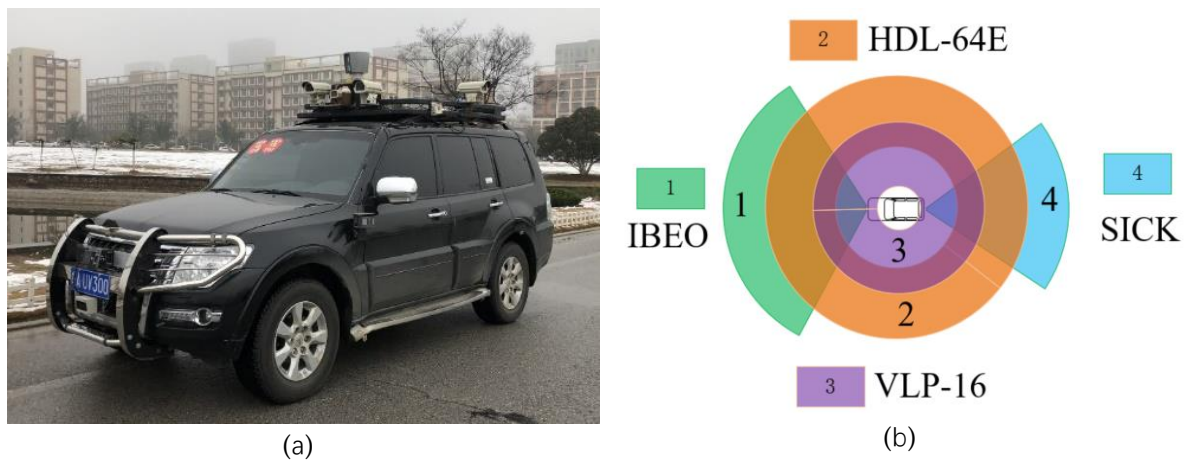
561 The simulation scenario shown in Figure 15 was established according to the real urban traffic
 562 scenario. Two typical traffic scenarios were selected to verify the adjustment effect of the priori
 563 reference trajectory on the predicted trajectory. Figure 16(a) shows the driving scene on the
 564 road, and Figure 16(b) shows the driving scene at the intersection. In the first scene, three
 565 reference trajectory intent segments were fitted to lane keeping (LK), lane change left (LCL),
 566 and lane change right (LCR), as shown by the blue curve in Figure 16(a). The historical
 567 observation vector of the target vehicle denoted the network input, and it was unchanged; the
 568 output network vector was converted according to three Prediction Reference Baseline to
 569 obtain three predicted trajectories, as shown by the green curve in Figure 16(c). In Figure 16(b),
 570 the intersection driving scenario is presented, where two Prediction Reference Baseline intent
 571 segments of go straight (GS) and turn right (TR) are fitted respectively; the converted network
 572 output results are shown by the green curve in Figure 16(d). Since the network learns the
 573 relative relationship between the historical and Prediction Reference Baseline, even at the same
 574 network input, the predicted trajectory will be affected by the Prediction Reference Baseline.
 575 The experimental results prove that the priori knowledge about the driving scene can be used
 576 to adjust the predicted trajectory effectively based on the Prediction Reference Baseline.

577 3.4. Real-World Urban Traffic Scenarios

578 3.4.1. Experimental Platform Construction

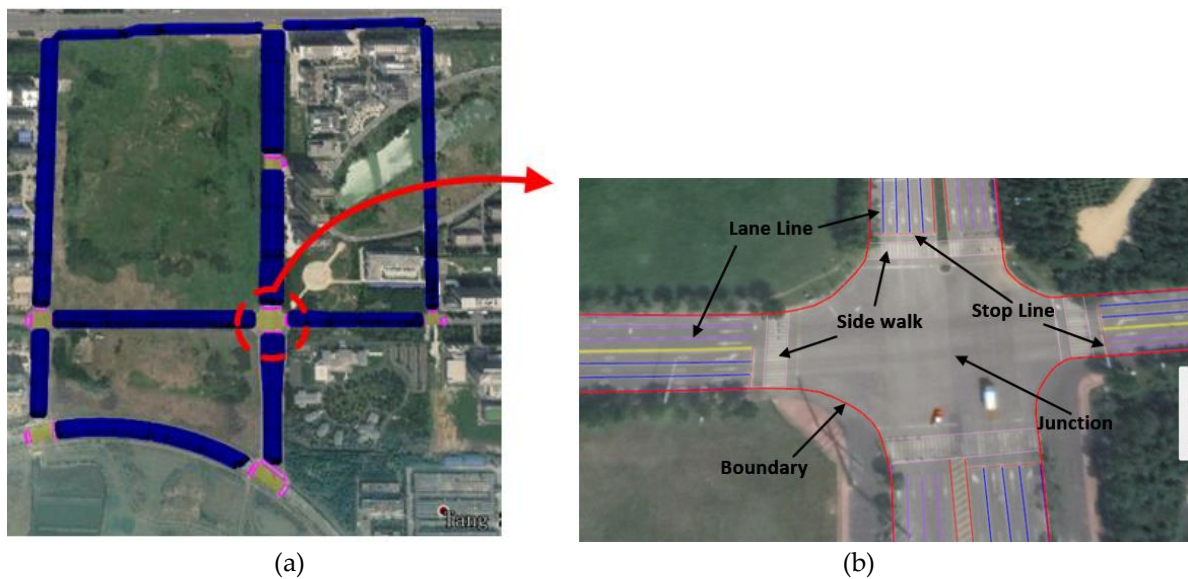
579 In order to verify if the simulation results obtained in coincide well with the real-world scenario
 580 results, an instrumented vehicle was used to collect data, as shown in Figure 17(a). The vehicle
 581 loading sensors included an IBEO four-layer laser scan instrument, a Velodyne HDL-64E lidar,
 582 two high-resolution cameras, and a differential GPS/INS (SPAN-CPT) system. The sensor
 583 configuration of the vehicle and its sensing range are shown in Figure 17(b). The differential
 584 GPS module provided the information on the position, speed, and heading of the ego vehicle.
 585 Based on our previous work [37], moving obstacles were detected and tracked by a four-layer
 586 laser scanner, which was located at the front of the vehicle. According to the space-time
 587 relationship between the moving obstacles, such as pedestrians and vehicles, and experimental
 588 vehicles, the position, speed, size, and type of the sports vehicles can be measured. We

589 conducted a real vehicle experiment in Hefei, Anhui Province, China. The test road is shown
 590 in Figure 18(a). The prediction model was exemplarily implemented on NVIDIA Xavier
 591 platform using the C++ programming language.



592 Figure 17. Experimental platform: (a) The Pioneer IV autonomous vehicle; (b) Perception range of the
 593 autonomous vehicle.

594 Before conducting the actual vehicle experiment, the high-resolution maps were collected to
 595 establish based on our experimental vehicle. There were more than 1,140 road entities on the
 596 map, including the stop signs, lane markings, and lane lines, covering approximately 8 km of
 597 the roadways (as Figure 18 shows).

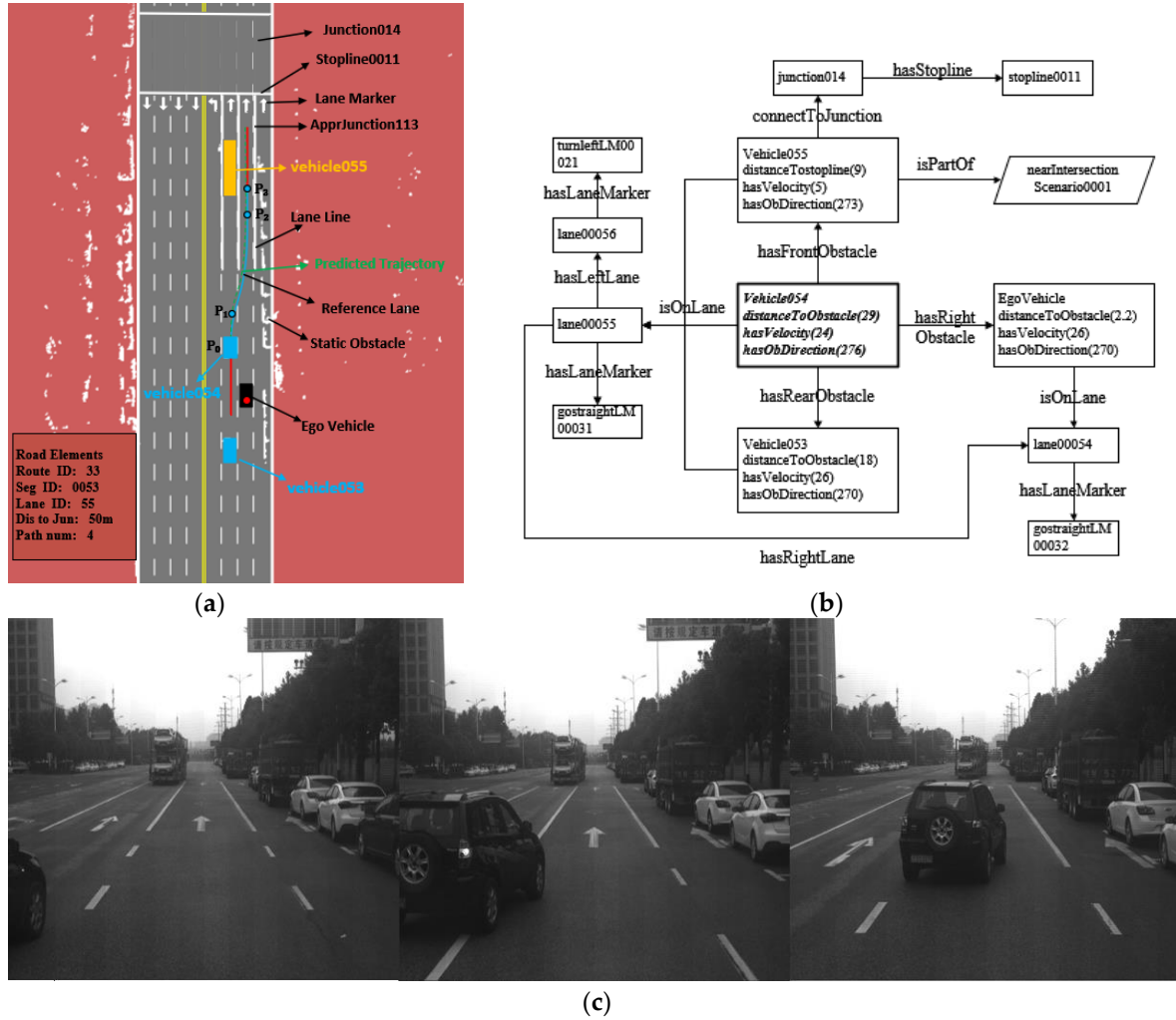


598 Figure 18. Testing roadway layout: (a) The high-resolution map of the experimental roadway; (b) An enlarged
 599 view of the map data.

600 3.4.2. Field Test and Discussion

601 The experimental driving route was located on a typical urban roadway, with a total length of
 602 about 4.7 km. It includes multiple intersections, Y-shaped intersections, T-shaped intersections,
 603 and other common urban road scenarios. Due to the long experimental route and a large number

604 of scenes encountered, it was inconvenient to conduct the prediction process for each scene.
 605 Therefore, two typical scenes were selected for detailed trajectory prediction process analysis.



606 Figure 19. The results of Scenario 1: (a) Trajectory prediction interface; (b) Scenario reasoning;
 607 (c) Experimental scenarios.

608 In Scenario 1, vehicle054 was on the road. The input conditions of the scene evaluation module
 609 are shown in Figure 17(b). In front of the target vehicle, there was a large truck denoted as
 610 vehicle055 that was moving with a speed of 5 km/h. At that time, the speed of vehicle054 was
 611 24 km/h. The calculated value of the TIV was less than the deceleration threshold. Therefore,
 612 it was judged that the target vehicle would have an intension to change lane. Vehicle054 was
 613 driving on lane00055, which was a straight lane. Through an associated search in the
 614 conceptual ontology model of the driving scene, it was learned that the right lane was also a
 615 straight lane, and the lane line was a white dotted line; the prolog rule of legality is expressed
 616 as follows:

617 $legalToRight(target, true): targetVehicle(target), isOnLane(target, Lane), hasRightLine(Lane, Line),$
 618 $hasLineType(Line, "dotted_white").$

619 The next section of the target vehicle to travel was the intersection, and the distance to the
 620 intersection was greater than 30 m, so the effectiveness of changing lanes was satisfied; thus,

621 the lane change did not affect the current target of the target vehicle; the prolog rule of
622 reasonableness is as follows:

623 *reasonableToRight(target,true): targetVehicle(target), currentRoadState(target,"ApprJunction"),*
624 *isOnSegment(target,Seg), connectToJunction(Seg,Junc), intersection(Junc), connectToStopLine(Seg,SL),*
625 *distToStopLine(SL,DL), DL >= 30.*

626 The autonomous vehicle was driving in the right back region of the target vehicle, and the TTC
627 and TIV values were both less than the corresponding acceleration threshold but greater than
628 the corresponding parking threshold; the prolog rule of safety is as follows:

629 *safeToRight(target,true): targetVehicle(target), hasRightObstacle(target,null),*
630 *hasRightFrontObstacle(target,null), hasRightBackObstacle(target,egovehicle).*

631 The final prolog rule is as follows:

632 *canChangeToRight(target,true): safeToRight(target,true), reasonableToRight(target,true), legalToRight*
633 *(target,true).*

634 After obtaining the driving intention of the target vehicle, the prior reference trajectory (the
635 blue curve in Figure 17(a)) was fitted, and the historical trajectory was transformed into Frenet
636 coordinates based on the prior reference trajectory and then fed to the LSTM network input;
637 the predicted trajectory is shown by the green dotted line in Figure 20(a). The trajectory
638 prediction results of vehicle054 could effectively reduce the reaction time of autonomous
639 vehicle while avoiding collisions caused by vehicle054 cutting in.

640 In Scenario 2, vehicle121 was in the pre-intersection scenario. The input conditions of the
641 scenario evaluation module are shown in Figure 20(b). The current speed of vehicle121 was
642 24 km/h, and the lane it traveled was lane000103, which was a right-turn lane. In this scenario,
643 the main factor affecting the target vehicle's driving intention was the traffic light. The prolog
644 rule of legality is as follows:

645 *legalToTurnRight(ego,acc): targetVehicle(target), currentRoadState(target,"ApprJunction"),*
646 *isOnSegment(target,Seg), connectToJunction(Seg,Junc), intersection(Junc), hasTrafficLight(Junc,TR),*
647 *hasLightColor(TR,"green"), connectToStopLine(Seg,SL), distToStopLine(SL,DL), DL = < 0*

648 The target vehicle was on the right turn, and the prolog rule of reasonableness is as follows:

649 *reasonableToLeft(ego,true): egoVehicle(ego), currentRoadState(ego,"ApprJunction"),*
650 *isOnSegment(ego,Seg), connectToJunction(Seg,Junc), intersection(Junc), connectToStopLine(Seg,SL),*
651 *distToStopLine(SL,DL), DL >= 30.*

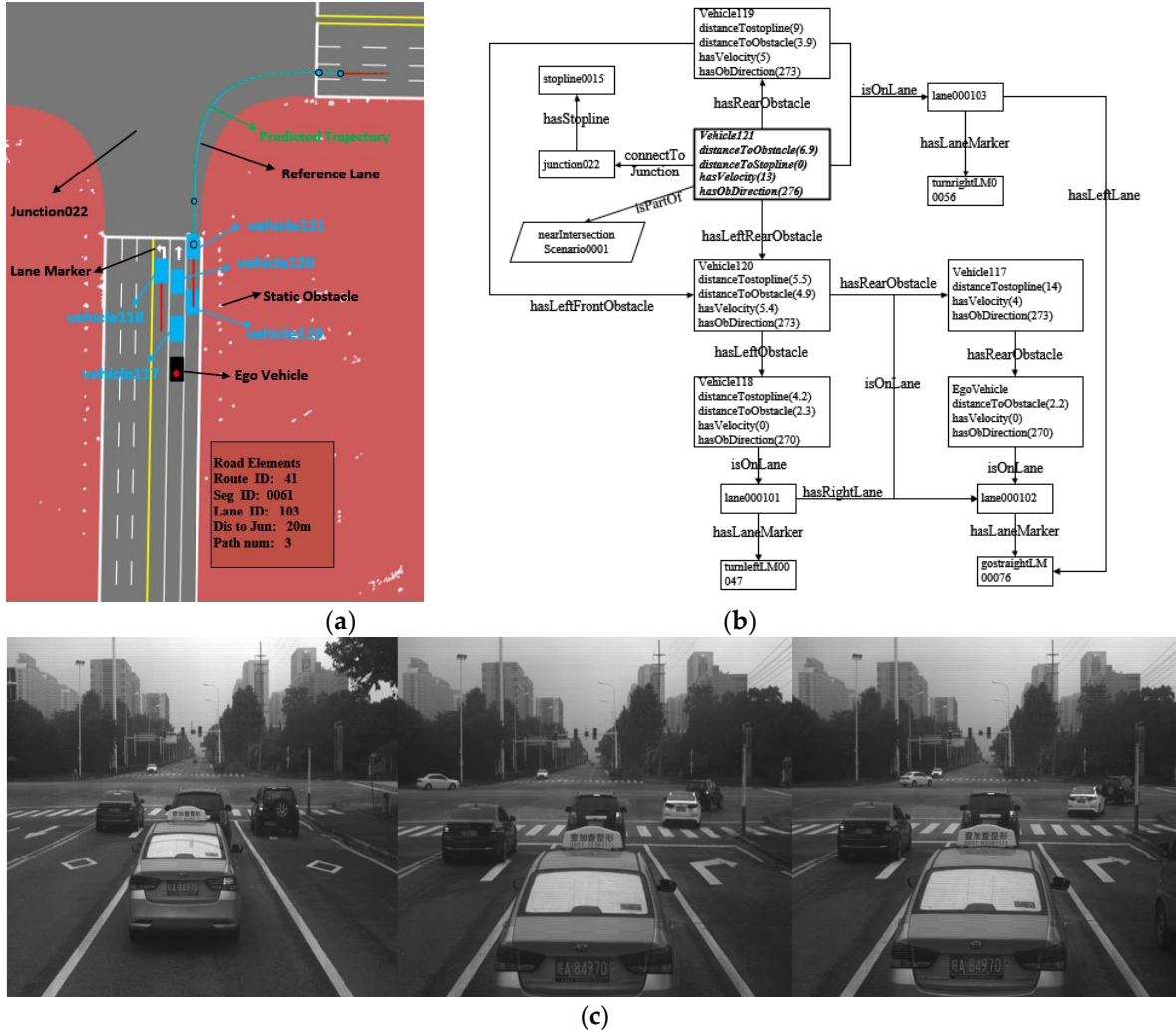
652 The final rule of safety is as follows:

653 *safeToTurnRight(target,true):-*
654 *targetVehicle(target),hasFrontObstacle(target,null),hasRightFrontObstacle(target,null),hasRightBackObstac*
655 *le(target,null).*

656 The final rule is expressed as:

657 $canTurnRight(target, true): \quad safeToTurnRight(target, true), \quad reasonableToTurnRight(target, true),$
 658 $legalToTurnRight (target, true).$

659 The blue curve in Figure 20(a) represents the prior reference trajectory fitted based on the turn
 660 right driving intention. The predicted trajectory is shown by the green dotted line in Figure
 661 20(a).



662 Figure 20. The results for Scenario 2: (a) Trajectory prediction interface; (b) Scenario reasoning;
 663 (c) Experimental scenarios.

664 The experimental results of Scenarios 1 and 2 verify that the proposed LSTM network can
 665 effectively combine the prior and posterior knowledge in the driving scene, and the lane change
 666 behavior can be predicted before the variation of vehicle kinemics. The proposed LSTM
 667 network can be iteratively adapted to a driving scenario without manual annotation during the
 668 network training, which significantly reduces the training complexity and solves the sparse
 669 data problem. Due to the unique combination of knowledge reasoning, the proposed prediction
 670 model can make a more accurate and reasonable estimation of future trajectories of surrounding
 671 vehicles than the existing models in different environments.

672 **4. Conclusions**

673 This paper combines a maneuver-based and learning-based trajectory prediction models and
674 proposes an improved trajectory prediction model based on the LSTM neural network driven
675 by driving knowledge. In order to achieve better use of a prior driving knowledge in driving
676 scenarios and solve the problem of the combinatorial explosion caused by a large number of
677 conditional attributes, the multi-source and heterogeneous information of the driving scenario
678 is modeled based on ontology, and a driving knowledge base, including the driving experience
679 and traffic rules, is constructed. Then, the conditional attributes that affect driving intentions
680 are classified and analyzed from the perspectives of safety, legitimacy, and reasonableness, and
681 situation parameters in the horizontal and vertical directions are generated by the deterministic
682 scene evaluation method. Finally, using the obtained situation parameters and the driving
683 knowledge base, the driving intention is inferred based on the prolog online reasoning system.
684 In order to make the prediction results effectively combine the posterior knowledge and solve
685 the problem of insufficient adaptability of the existing learning-based prediction models, this
686 paper converts the driving intention of the target vehicle into a prior reference trajectory, and
687 the Frenet coordinates based on prior reference trajectory are used as a coordinate frame for
688 the LSTM neural network. The prior driving knowledge existing in the driving scene can be
689 used to adjust the predicted trajectory in the form of the prior reference trajectory without
690 increasing the network complexity but ensuring efficient operation of the proposed model on
691 an embedded platform.

692 The proposed prediction model was verified by simulations and experiments. The simulation
693 results showed that the prior reference trajectory could effectively adjust the output of the
694 LSTM neural network, making the predicted trajectory meet the constraints of the prior
695 knowledge in a driving scenario. The real-world-experiment results show that the proposed
696 prediction model can significantly reduce the computing performance requirements while
697 ensuring real-time performance on the embedded platform. Also due to the full combination of
698 prior and posterior knowledge in the driving scene, the target vehicle's lane-changing
699 behaviour can be predicted on average 2.05 s (for LCL) or 2.71 s (for LCR) in advance, and
700 the precision can be improved by 12.5% for long-term predictions and is more robust, flexible,
701 and adaptive in complex traffic scenarios.

702 Even though the proposed model has advantages in trajectory prediction, there are still some
703 limitations, such as that indexes of scenario assessment are not comprehensive enough. In order
704 to overcome this limitation, in future work, the evaluation index will be considered from the
705 perspective of human-vehicle interaction and multi-vehicle interaction. Furthermore, data from
706 a more complex scenario will be collected and used to verify the proposed prediction model.

707 **Data Availability**

708 The data used to support the findings of this study are available from the corresponding
709 author upon request.

710 **Conflicts of Interest**

711 The authors declare no conflicts of interest.

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726 References

- 727 [1] Stéphanie Lefèvre, D. Vasquez , and C. Laugier . A survey on motion prediction and risk assessment
 728 for intelligent vehicles. *ROBOMECH Journal* 1.1(2014):1-14.
- 729 [2] Dai, Shengzhe , L. Li , and Z. Li . Modeling Vehicle Interactions via Modified LSTM Models for
 730 Trajectory Prediction. *IEEE Access* (2019):38287-38296.
- 731 [3] Kaempchen N, Weiss K, Schaefer M, Dietmayer KCJ (2004) IMM object tracking for high dynamic
 732 driving maneuvers In: *Proc. IEEE intelligent vehicles symposium*, pp 825–830.
- 733 [4] Veeraraghavan H, Papanikolopoulos N, Schrater P (2006) Deterministic sampling-based switching
 734 Kalman filtering for vehicle tracking In: *Proc.IEEE intelligent transportation systems conference*, pp
 735 1340–1345
- 736 [5] Broadhurst, Adrian, Simon Baker, and Takeo Kanade. Monte Carlo road safety reasoning. *IEEE*
 737 *Proceedings. Intelligent Vehicles Symposium, 2005.. IEEE, 2005.*
- 738 [6] Bahram, Mohammad, et al. A combined model-and learning-based framework for interaction-aware
 739 maneuver prediction. *IEEE Transactions on Intelligent Transportation Systems* 17.6 (2016): 1538-
 740 1550.
- 741 [7] Ortiz, Michaël Garcia, et al. Behavior prediction at multiple time-scales in inner-city scenarios. 2011
 742 *IEEE Intelligent Vehicles Symposium (IV). IEEE, 2011.*
- 743 [8] Klingelschmitt, Stefan , et al. Combining behavior and situation information for reliably estimating
 744 multiple intentions. *Intelligent Vehicles Symposium IEEE, 2014.*
- 745 [9] Morris, Brendan , A. Doshi , and M. Trivedi . Lane change intent prediction for driver assistance: On-
 746 road design and evaluation. 2011 *IEEE Intelligent Vehicles Symposium (IV) IEEE, 2011.*
- 747 [10] Kumar P, Perrollaz M, Lefèvre S, Laugier C (2013) Learning-based approach for online lane change
 748 intention prediction In: *Proc. IEEE Intelligent Vehicles Symposium*, pp 797–802
- 749 [11] Zyner, Alex , et al. Long short term memory for driver intent prediction. 2017 *IEEE Intelligent*
 750 *Vehicles Symposium (IV) IEEE, 2017.*
- 751 [12] A. Alahi, K. Goel, V. Ramanathan, A. Robicquet, L. Fei-Fei, and S. Savarese, Social LSTM: Human
 752 Trajectory Prediction in Crowded Spaces, in 2016 *IEEE Conference on Computer Vision and Pattern*
 753 *Recognition (CVPR). IEEE, jun 2016, pp. 961–971.*
- 754 [13] D. J. Phillips, T. A. Wheeler, and M. J. Kochenderfer, Generalizable Intention Prediction of Human
 755 Drivers at Intersections, 2017 *IEEE Intelligent Vehicles Symposium (IV)*, pp. 1665–1670, 2017.
- 756 [14] F. Altché, and A. De La Fortelle, An LSTM network for highway trajectory prediction, *IEEE 20th*
 757 *International Conference on Intelligent Transportation Systems (ITSC)*, pp. 353-359, October 2017.
- 758 [15] C. Ding, W. Wang, X. Wang, and M. Baumann, A neural network model for driver’s lane-changing
 759 trajectory prediction in urban traffic flow, *Mathematical Problems in Engineering*, vol. 2013, 2013.
- 760 [16] J. Zheng, K. Suzuki, and M. Fujita, Predicting driver’s lane changing decisions using a neural network
 761 model, *Simulation Modelling Practice and Theory*, vol. 42, pp. 73–83, 2014.

- 762 [17] P. Kumar, M. Perrollaz, S. Lefevre, and C. Laugier, Learning-based approach for online lane change
763 intention prediction, in 2013 IEEE Intelligent Vehicles Symposium (IV). IEEE, jun 2013, pp. 797–802.
- 764 [18] S. H. Park, B. Kim, C. M. Kang, C. C. Chung and J. W. Choi, Sequence-to-Sequence Prediction of
765 Vehicle Trajectory via LSTM Encoder-Decoder Architecture, 2018 IEEE Intelligent Vehicles
766 Symposium (IV), Changshu, 2018, pp. 1672-1678.
- 767 [19] Xin, Long , et al. Intention-aware Long Horizon Trajectory Prediction of Surrounding Vehicles using
768 Dual LSTM Networks. 2018 IEEE International Conference on Intelligent Transportation Systems
769 (ITSC) IEEE, 2018.
- 770 [20] N. Deo and M. M. Trivedi, Multi-Modal Trajectory Prediction of Surrounding Vehicles with Maneuver
771 based LSTMs, 2018 IEEE Intelligent Vehicles Symposium (IV), Changshu, 2018, pp. 1179-1184
- 772 [21] Ding, Wenchao , and S. Shen . Online Vehicle Trajectory Prediction using Policy Anticipation
773 Network and Optimization-based Context Reasoning. 2019 International Conference on Robotics and
774 Automation (ICRA) IEEE, 2019.
- 775 [22] N. Deo and M. M. Trivedi, Convolutional social pooling for vehicle trajectory prediction, 2018,
776 arXiv:1805.06771. [Online]. Available: <https://arxiv.org/abs/1805.06771>.
- 777 [23] Dai S , Li L , Li Z . Modeling Vehicle Interactions via Modified LSTM Models for Trajectory
778 Prediction[J]. IEEE Access, 2019:38287-38296.
- 779 [24] Khakzar M , Rakotonirainy A , Bond A , et al. A Dual Learning Model for Vehicle Trajectory
780 Prediction[J]. IEEE Access, 2020, 8(99):21897-21908.
- 781 [25] Hummel, Britta, Werner Thiemann, and Irina Lulcheva. Scene understanding of urban road
782 intersections with description logic. Dagstuhl Seminar Proceedings. Schloss Dagstuhl-Leibniz-Zentrum
783 fr Informatik, 2008.
- 784 [26] Armand, Alexandre, David Filliat, and Javier Ibañez-Guzman. Ontology-based context awareness for
785 driving assistance systems. 2014 IEEE intelligent vehicles symposium proceedings. IEEE, 2014.
- 786 [27] Ralf Kohlhaas, Thomas Bittner, Thomas Schamm, and J Marius Zollner. Semantic state space for high-
787 level maneuver planning in structured traffic scenes. Intelligent Transportation Systems (ITSC), 2014
788 IEEE 17th International Conference on. IEEE, 2014: 1060–1065.
- 789 [28] Xinli, Geng , et al. A Scenario-Adaptive Driving Behavior Prediction Approach to Urban Autonomous
790 Driving. Applied ences 7.4(2017):426.
- 791 [29] Glaser S, Vanholme B, et al. Maneuver-Based Trajectory Planning for Highly Autonomous Vehicles
792 on Real Road With Traffic and Driver Interaction. IEEE transactions on Intelligent Transportation
793 Systems 2010,11(3): 589-606.
- 794 [30] N. Samyeul and A. Kyoungwan, Decision-Making Framework for Automated Driving in Highway
795 Environments, IEEE Transactions on Intelligent Transportation Systems, 2018,19(1): 58-71.
- 796 [31] Noh, Samyeul, Kyoungwan An, and Wooyong Han. Situation assessment and behavior decision for
797 vehicle/driver cooperative driving in highway environments. 2015 IEEE International Conference on
798 Automation Science and Engineering (CASE). IEEE, 2015.
- 799 [32] Hochreiter, Sepp, and Jürgen Schmidhuber. Long short-term memory. Neural computation 9.8 (1997):
800 1735-1780.
- 801 [33] US Department of Transportation, NGSIM: Next Generation Simulation, 2008, Available:
802 <http://www.ngsim.fhwa.dot.gov>. [Accessed: June 6, 2017].
- 803 [34] A. Bender, J. R. Ward, S. Worrall, and E. M. Nebot, Predicting driver intent from models of
804 naturalistic driving, in 2015 IEEE 18th International Conference on Intelligent Transportation Systems.
805 IEEE, 2015, pp. 1609–1615.
- 806 [35] Yoon, Seungje, and Dongsuk Kum. The multilayer perceptron approach to lateral motion prediction of
807 surrounding vehicles for autonomous vehicles. 2016 IEEE Intelligent Vehicles Symposium (IV). IEEE,
808 2016.
- 809 [36] K. Messaoud, I. Yahiaoui, A. Verroust-Blondet and F. Nashashibi, Non-local Social Pooling for
810 Vehicle Trajectory Prediction, 2019 IEEE Intelligent Vehicles Symposium (IV), Paris, France, 2019,
811 pp. 975-980.
- 812 [37] Huang, Rulin, et al. A practical point cloud based road curb detection method for autonomous vehicle.
813 Information 8.3 (2017): 93.